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Version V2.0

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Analysis, Interpretation and Recognition of 2D (touch) and 3D (Gestures) for New Man-Machine Interactions



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CHAP. 16 : Neural Networks

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_Chapitre 1

Introduction: understand the problematic of gesture interaction

_Chap. 1 | 2D and 3D Action/Gesture recognition: a challenge?

- Introduction: understand the problematic of gesture interaction
 - What is a gesture: the different natures of gestures
 - Human Computer Interaction: new opportunities
- Gesture recognition: Isolated Gestures Classification (segmented)
 - Overview of the task: recognizing isolated gestures (The overall pattern recognition process)
 - Machine Learning and Pattern recognition: a short overview of some existing techniques
 - Gesture classication: "Time-series" approaches
 - Pre-segmented Action Recognition: Skeleton based and "Statistical" approaches
- Gesture recognition in real-time streaming (non segmented)
 - Overview of the task: recognizing in real-time streaming
 - Non-segmented Action Recognition: Example of one approach [Boulahia 2017]
 - Presentation of experimental results using Kinect and Leap Motion
- Early Gesture recognition



_Chap. 1 | 2D gesture sensors: pen-based and touch-based gestures

- Pen-based gesture interaction
 - Device platforms
 - Smartphone
 - Digital Pen
 - Tablet PC
 - Electronic Whiteboard
 - · ...













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$_{\mbox{\tiny Chap.\,1}}\mbox{\mid}~$ 2D gesture sensors : pen-based and touch-based gestures

- Touch-based gesture interaction (touch screen)
 - Multi touch based interaction (ex: whiteboarding solution...)
 - Multi-user based interaction (ex: surface table, surface Hub...)
- Tracking technology: capacitive touch screen display,ultrasound, infrared...









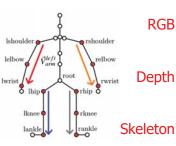






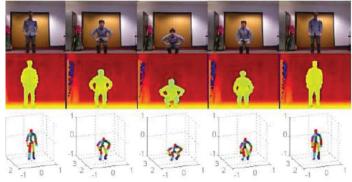
_chap. 1 | 3D gesture sensors: whole body gestures recognition

- Dynamic whole body gestures recognition
 - Wide range of application fields: such as video surveillance, sport video analysis, humancomputer interaction, computer animation and even health-care.
- Two main groups of approaches
 - RGB + Depth image recognition
 - Skeleton-based action recognition
- Sensor technologies
 - Emergence of Kinect like sensors (2010)





Crouching





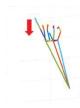
_chap. 1 | 3D gesture sensors: Hand Gesture

- Dynamic hand gestures
 - using skeleton joint data
- Sensor technologies
 - the Leap Motion device
 - Intel's RealSense depth-sensing 3D camera
 - Depth sensor + camera
- Few existing applications



















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_Chapitre 2

Inputs: time-series

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_Chap. 2 | 2D gesture inputs: Pen-based and touch-based gestures

On-line

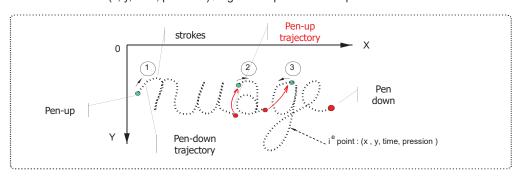






Data input







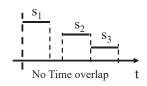
_Chap. 2 | 2D gesture inputs: Multi-stroke and Multi-touch

Multi-stroke and Multi-touch Gesture



Multi-stroke (sequence of strokes)

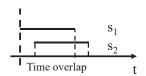




Multi-touch (several strokes in //)







- Several trajectories to consider
 - Strokes are written in sequence
 - Shape
 - Spatial relation

- Strokes are synchronized or partial synchronized
 - Shape
 - Spatial relation
 - Temporal relation



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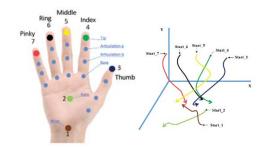
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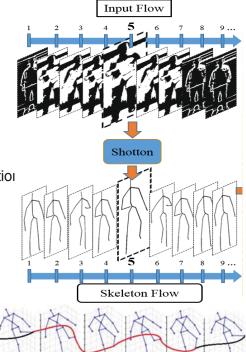
_chap. 2 | 3D gesture inputs

- Two main groups of approaches:
 - RGB-D based => input data = a sequence of frames



- Skeleton based
 - By using Kinect, LeapMotion
 - a sequence of 3D points = trajectory, angular information

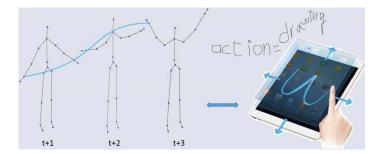






_chap. 2 | Inputs: Trajectories / One generic approach for 2D/3D gesture recognition?

- 3D gesture
 - A robust approach : Skeleton based approach
 - capture the essential structure of a subject in an easily understandable way
 - robust to variations in viewpoint and illumination
 - skeleton data consist in trajectories of the body joints
- Trajectories: a unified way to consider gestures
 - Same data type: trajectories or signal
 - 3D gesture trajectories may be processed similarly to 2D trajectories
- Moreover from Graphonomic point of view
 - 3D and 2D gestures : a human is the performer





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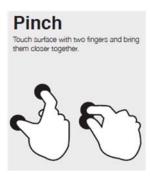
_Chapitre 3

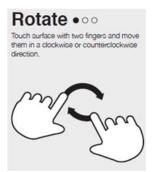
Introduction to Gesture Interaction

_Chap. 3 | Gesture interaction

- General Introduction based on [Zhaoxin Chen 2016]
 - Touch gesture examples[1]







[1] Touch gesture reference guide, Luke Wroblewski, http://www.lukew.com/



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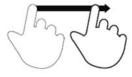
_Chap. 3 | Gesture interaction: Mono Stroke

Development of gesture interaction





Tap



Drag



Handwritten character



_chap. 3 | Gesture interaction: Multi-Stroke

Development of gesture interaction







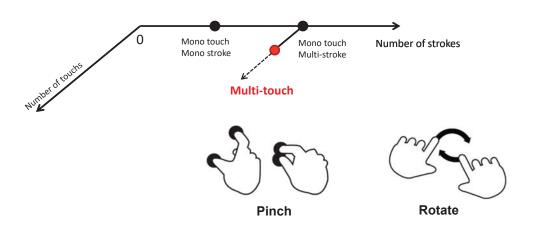




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_chap. 3 | Gesture interaction

Development of gesture interaction

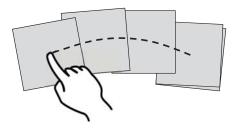




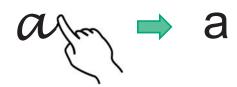
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_chap. 3 | Gesture interaction: Direct and Indirect commands

Two types of interactions



Direct manipulation



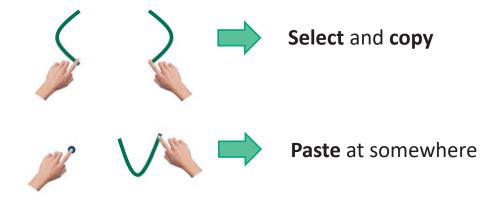
Indirect command



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_chap. 3 | Gesture interaction: Direct and Indirect commands

• What if a user wants to use the multi-touch gesture to make a command instead of manipulation.

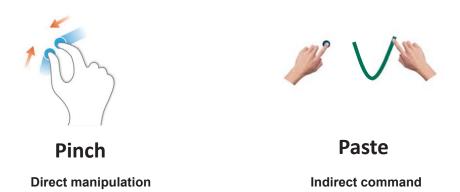


How to recognize a multi-touch gesture as indirect command?



_Chap. 3 | Gesture interaction: Direct and Indirect commands

• Is it possible to merge these two interactions into a same interface



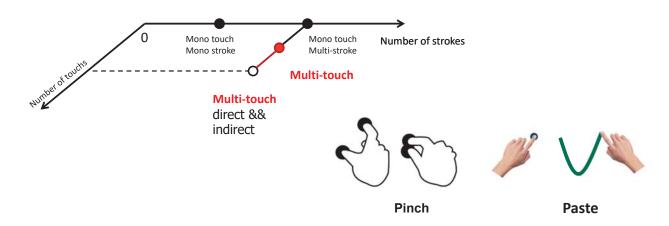
How to support these two interactions in a same context?



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_chap. 3 | Gesture interaction: multi-touch gestures

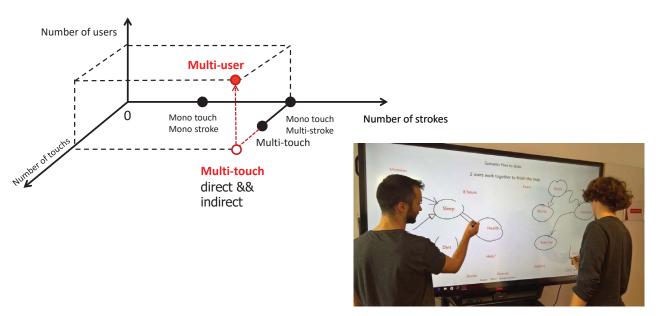
- Open more possibilities to use multi-touch gestures
 - complex gesture for indirect commands
 - mix the direct manipulation and indirect command





chap. 3 | Gesture interaction: Multi-user interaction

- Multi-user interaction
 - to deal with several gestures in the same time





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_chap.3 | Perspective: future of Pen and Touch interaction [Pfeuffer CHI 2017]

- Example of novel way of interaction: Thumb + Pen interactions
 - Support simultaneous pen and touch interaction, with both hands
 - allow changing the mode of the pen
 - changing the mode that applies to the pen conventions.
 - additional navigation functionality

• ...

[Pfeuffer 2017] Thumb + Pen Interaction on Tablets Ken Pfeuffer, Ken Hinckley, Michel Pahud, Bill Buxton Microsoft Research, Redmond, WA, USA Interactive Systems, Lancaster University, UK



Figure 1: Thumb + Pen interaction enables simultaneous bimanual pen+touch while holding a tablet with the off-hand.





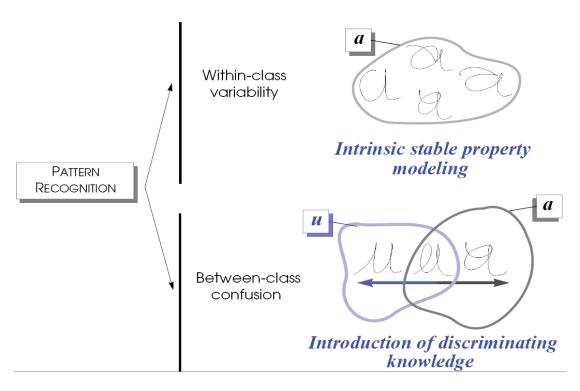
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_Chapitre 4

Intra/inter -class variability (shape, spatial and temporal)

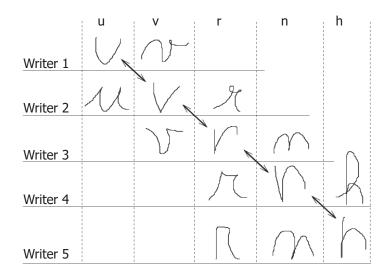
_chap. 4 | Intra/Inter -class: shape variabilities





_chap. 4 | Intra/Inter -class: shape variabilities

- Writer dependent versus Writer-independent recognizer
 - Resource cost
 - Ambiguity of characters between different writers
 - No ambiguity for each writer
 - [Mouchère07]

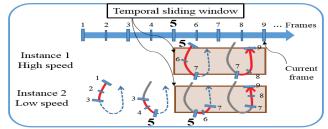




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_chap. 4 | Intra/Inter —class: temporal and spatial variabilities

- Temporal variability
 - Occurs when subjects perform gestures with different speeds
- Inter-class spatial variability
 - Different gesture classes are likely to result in different amount of displacements
- Intra-class spatial variability
 - Same action class with different amount of displacements
 - In some applications, capturing such intra-class variabilities might be desirable as it brings additional information and could allow for different interpretations of the same class of gesture.
 Othewise need to must be neutralized.



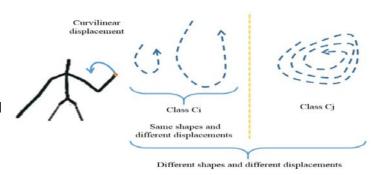


Fig. 1. Illustration with a single joint trajectory of intra-class spatial variability within a class Ci (left) and inter-class spatial variability between Ci and Cj (right).



__Chap. 4 | Gesture Recognition: a transversal challenge

Application

- Human computer interaction
- Pattern recognition

- Animation
- 3D/2D actions
- · Map view
- · Document composition
- · Mono touch & Multi-touch
- Direct & Indirect command
- Multi-user interaction
- Isolated multi-touch gesture recognition
- · Non segmented gesture recognition
- · Early recognition for touch gesture
- Multi-user gesture segmentation and recognition



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_Chapitre 5

Gesture recognition: Isolated Gestures Classification (segmented)

_chap. 5 | 2D and 3D Action/Gesture recognition: a challenge?

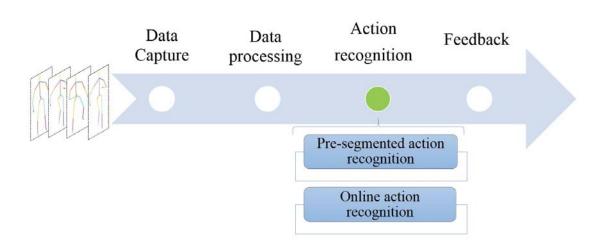
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_Chap.5 | Overview of the task: generic flowchart

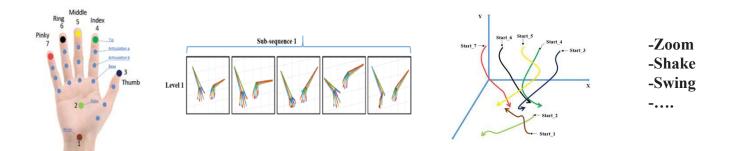
* Human action recognition



_Chap. 5 | The overall pattern recognition process (segmented gestures)

• The overall process for segmented dynamic gesture recognition (hand gesture illustration)







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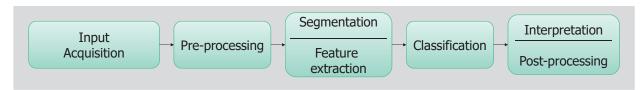
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__Chap. 5 | The overall pattern recognition process: Pattern Recognition

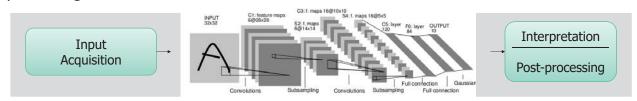
Overview



Classical Process

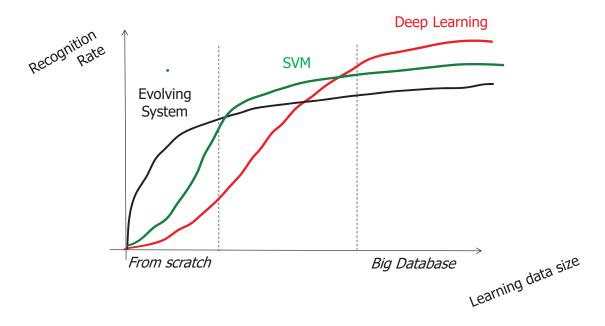


With Deep Learning





Overview



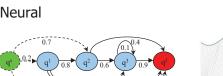


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_Chap. 5 | The overall pattern recognition process: Pattern Recognition

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- "Dynamic /Time-series" approaches (AMRG-AIR)
 - Input: Handle the sequential data with variable lengths
 - Elastic Matching (Dynamic Time Wrapping, DTW)
 → similarity between two sequences
 - Hidden Markov Model (HMM)
 - Recurrent neural networks (RNNs), Time, Space Delay Neural Network (TDNN, SDNN)
 - long short-term memory (LSTM) network

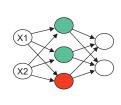


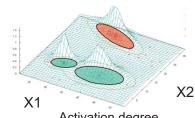


- Input : Feature vector (low level representation)
 - Recognition system:

Classifier (learning and generalization phase)

- —Support Vector Machine (SVM)
- —Neural Network (MLP, RBF,....),
- -Fuzzy Inference System (FIS),
- —Decision tree, ...
- CNN: Convolutional Neural Networks





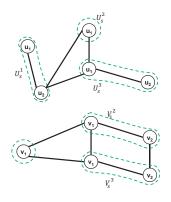
Activation degree

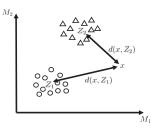


- "Structural" approaches
 - Input
 - Primitives → feature vector (high level representation)
 - Based on fine analysis of the pattern
 - Recognition system: Classifier (learning and generalization phase)
 - Possibly the same classifier as "statistical" approaches
 - Fuzzy Inference System (FIS), Decision Tree, ...
 - Advantage: transparent system, possible optimization
 Drawback: more difficult to design



- K nearest neighbors (KNN) (without Learning phase ...)... need to define a distance (ex: DTW...)
- Hybrid Approaches: HMM + NN







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_Chapitre 6

Gesture classication: "Time-series" approaches

chap. 6 | Gesture classication: "Time-series" approaches

- Many fields to consider time-ordered Series of Data:
 - Motion/Gesture

 - M. Morel, C. Achard, R. Kulpa, and S. Dubuisson, "Automatic evaluation of temporal errors", Image and Vision Computing, vol. 64, pp. 67–78, 2017.

 M. T. Pham, R. Moreau, and P. Boulanger, "Three-dimensional **gesture comparison** using curvature analysis of position and orientation," in EMBC'10, pp. 6345–6348, IEEE, 2010.

 F. Zhou and F. D. la Torre Frade, "Canonical time warping for alignment of **human behavior**," in Advances in Neural Information Processing Systems Conference (NIPS), December 2009.
 - Handwriting

 - I. Guler and M. Meghdadi, "A different approach to off-line handwritten signature verification using the optimal dynamic time warping algorithm," Digital Signal Processing, vol. 18, no. 6, pp. 940–950, 2008.
 Mitoma, H., S. Uchida, and H. Sakoe. Online character recognition based on elastic matching and quadratic discrimination. in Eighth International Conference on Document Analysis and Recognition. 2005. p. 36-40 Vol. 31.
 Niels, R. and L. Vuurpijl, Dynamic time warping applied to Tamil character recognition. Eighth International Conference on Document Analysis and Recognition, 2005: p. 730-734 Vol. 732.
 - Biological systems
 - B. S. Raghavendra, D. Bera, A. S. Bopardikar, and R. Narayanan, "Cardiac arrhythmia detection using dynamic time warping of ECG beats in e-healthcare systems," in IEEE International Symposium on a World of Wireless, Mobile and Multimedia Networks, pp. 1–6, IEEE, 2011.
 - Audio (speech or music) signals.

 - G. Kang and S. Guo, "Variable sliding window DTW **speech** identification algorithm," in Ninth International Conference on Hybrid Intelligent Systems, pp. 304–307, IEEE, 2009.

 Ning Hu, R. Dannenberg, and G. Tzanetakis, "Polyphonic audio matching and alignment for **music** retrieval," in IEEE Workshop on Applications of Signal Processing to Audio and Acoustics, pp. 185–188, IEEE, 2003.



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_Chap. 6 | Gesture classication: "Time-series" approaches

- Time-series challenges
 - Difficulties: length variability
 - requiring their temporal alignment as a pre-processing step
 - To learn a Model
 - to derive a single model from a set of signals corresponding to several instances of the same physical process.



- Hidden Markov Model (HMM)
- Dynamic programming (DP) / Dynamic time warping (DTW)
 - [Morel 2017] Marion Morel, Catherine Achard, Richard Kulpa, and Séverine Dubuisson. Time-series averaging using constrained dynamic time warping with tolerance. Pattern Recognition, 2017.









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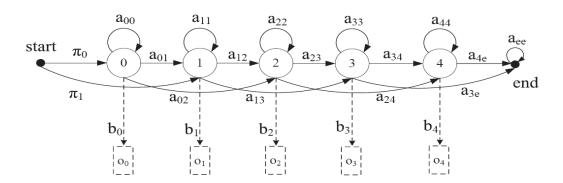
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_Chapitre 7

Hidden Markov Model

_Chap. 7 | Classification: Hidden Markov Models (HMM)

- Hidden Markov Models: approach inspired from speech recognition
 - deal with sequence of observations
 - find application in practically all ranges of the statistic pattern recognition
- HMMs
 - Generalization of homogeneous Markov chains with a stochastic process on two stochastic processes
 - Sequence of the states is produced by the transition probabilities a;
 - At each state is associated an emission probability b_i(o)





- Definition
 - An HMM is a double stochastic process
 - an underlying stochastic process generates a sequence of states

$$q_1, q_2, \ldots, q_t, \ldots q_T$$

Where

t: discrete time, regularly spaced T: length of the sequence $q_t \in Q = \{q_1, q_2, ..., q_N\}$

N: the number of states

each state emits

an observation according to a second stochastic process:

$$o_t \in O = \{o_1, o_2, \dots o_M\}$$

 $o_i : a \ discrete \ symbol$

M: number of symbols

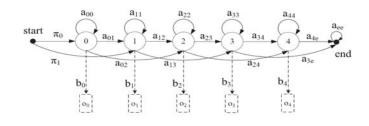
- Specification of an HMM $\lambda = (\Pi, A, B)$
 - A the state transition probability matrix

$$a_{ij} = P(q_{t+1} = j/q_t = i)$$

■ B - observation probability distribution

$$b_{ij} = P(o_t = o^j / q_t = q^i)$$

■ Π - the initial state distribution



$$b_{ij} \geq 0$$
 and $\sum_{j=1}^{M} b_{ij} = 1$

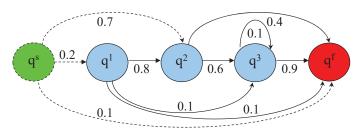


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_Chap. 7 | HMM: example

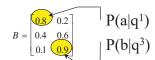
Example of non ergodic model (left-right model)



- 3 states + 1 starting state q^s + 1 final state q^f
 - q^s and q^f are non emitting states
- Assume there are 2 symbols to observe O = {o¹=a, o²=b}
 - Example of possible observation sequence: "a b b b"

$$\Pi = \begin{bmatrix} 0.2 \\ 0.7 \\ 0 \\ 0.1 \end{bmatrix}$$

$$A = \begin{bmatrix} 0 & 0.8 & 0.1 & 0.1 \\ 0 & 0 & 0.6 & 0.4 \\ 0 & 0 & 0.1 & 0.9 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Initiale state probabilities

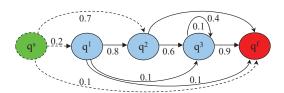
Transition state probabilities

Observation symbol probabilities

[C. Viard-Gaudin]

_Chap. 7 | HMM: example

- The most probable state sequence is:
 - q², q³ resulting in the symbol sequence "bb".
 - But this sequence can also be generated by other state sequences, such as q^1 , q^2 .



08 02 0.4 0.6 0.1 0.9

- Computation of the likelihood of an observation sequence:
 - Given X = ``aaa'' compute the likelihood for this model : $P(aaa \mid \lambda)$
 - The likelihood $P(X \mid \lambda)$ is given by the sum over all possible ways to generate X.

State sequence	Init	Obs a	Trans	Obs a	Trans	Obs a	Trans	Joint probability
q ¹ q ² q ³	0.2	0.8	0.8	0.4	0.6	0.1	0.9	0.0027648
q ¹ q ³ q ³	0.2	0.8	0.1	0.1	0.1	0.1	0.9	0.0000144
q²q³q³	0.7	0.4	0.6	0.1	0.1	0.1	0.9	0.0001512
						P(aaa	a λ) =	0.0029304



[C. Viard-Gaudin] © eric.anquetil@irisa.fr

_Chap. 7 | HMM: basic problems

- The 3 basic problems for HMMs
 - Problem 1 : Evaluate the probability of an observation sequence (Forward-Backward algorithm)
 - Given O = (o1,o2, ... oT) and a model λ
 - How to efficiently compute the probability $P(O \mid \lambda)$ of a given observation sequence?
 - Problem 2 : Find out the most likely state sequence (Viterbi algorithm)
 - Given O = (o1,o2, ... oT) and a model λ
 - how to efficiently find the optimal state sequence for which the probability of a given observation O = (o1,o2, ... oT) is maximum.
 - Problem 3 : Learning (Baum-Welch algorithm)
 - Given a set of training sequences $\{O = (o1,o2, \dots oT)\}$, how to efficiently estimate the parameters of a model $\lambda = (\Pi$, A, B) according to the maximum likelihood criterion.



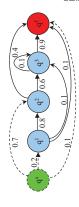
_Chap. 7 | HMM: Viterbi algorithm

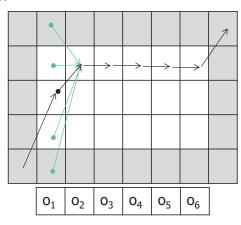
- Viterbi algorithm: Solution by Dynamic Programming
 - Define δ_t(i) the highest probability path ending in state qⁱ

•
$$\delta_t(i) = \max_{q_1, q_2, ..., q_t = q^i} p_1, o_1, o_2, ...o_t \mid \lambda)$$

- By induction:
 - . $\delta_{t+1}(k) = \max_{1 \le i \le N} [\delta_t(i) \ a_{ik}]$. $b_k(o_{t+1})$, with $1 \le k \le N$
 - . Memorize $\Psi_{t+1}(k) = arg max(\delta_t(i) a_{ik})$

1<i<N







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_Chap. 7 | HMM: Viterbi algorithm

- Viterbi algorithm: Solution by Dynamic Programming
 - 1. Initialization

For
$$1 \le i \le N$$
 { $\delta_1(i) = \pi_i \times b_i(o_1)$; $\Psi_1(i) = 0$;}

2. Recursive computation

For
$$2 \le t \le T$$

$$\begin{split} \text{For } 1 &\leq j \leq N \\ \delta_t(j) &= \max \left[\delta_{t\text{-}1}(i) \ a_{ij} \right] \text{. } b_j(o_t); \\ 1 &\leq i \leq N \end{split}$$

$$\Psi_t(j) &= \text{arg max}(\delta_{t\text{-}1}(i) \ a_{ij}); \\ 1 &\leq i \leq N \end{split}$$

3. Termination

$$\begin{aligned} P^* &= max[\delta_t(i)]; \\ &1 \leq i \leq N \\ q^*_T &= arg \; max[\delta_T(i)]; \\ &1 \leq i \leq N \end{aligned}$$

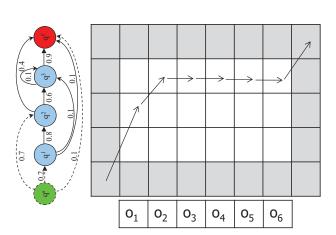
4. Backtracking

For t=T-1 down to 1 {
$$q^*_{t} = \Psi_t(q^*_{t+1})$$
; }

 $\ensuremath{\mathsf{P}}^*$ gives the required state-optimized probability

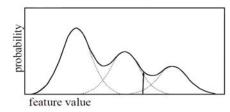
 $\Gamma^* = (q_1^*, q_2^*, ..., q_T^*)$ is the optimal state sequence





chap. 7 HMM: discrete versus continuous

- Different types of HMMs on the basis of the kind of symbols:
 - Discrete HMMs
 - Number of possible symbols, probability of the symbols in matrix
 - quantization errors at boundaries
 - relies on how well Vector Quantization (clustering) partitions the space
 - sometimes problems estimating probabilities when unusual input vector not seen in training
 - Continuous HMMs
 - Probabilities of symbols in continuous form; distribution density
 - Example: the emission probability is expressed with mixtures of Gaussians.

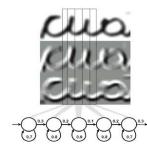




Sequence of primitives [Viard Gaudin]



Discrete HMM 5 clusters [Viard Gaudin]



[Juan 04]

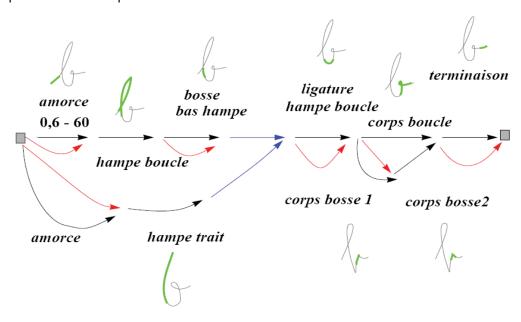
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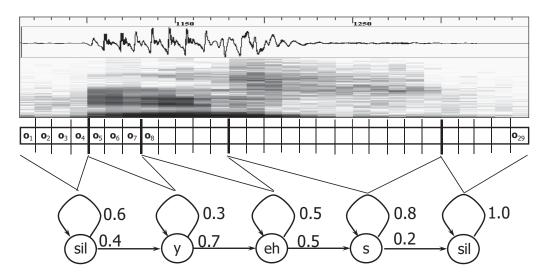
_Chap. 7 | HMM: example

- Another explicit segmentation : example of an on-line approaches
 - Discrete Emission probability
 - Sequence based on primitives





■ Example of using HMM for word "yes" [John-Paul Hosom 2009]



 $b_{\text{sil}}(\mathbf{o}_1) \cdot 0.6 \cdot b_{\text{sil}}(\mathbf{o}_2) \cdot 0.6 \cdot b_{\text{sil}}(\mathbf{o}_3) \cdot 0.6 \cdot b_{\text{sil}}(\mathbf{o}_4) \cdot 0.4 \cdot b_{\text{y}}(\mathbf{o}_5) \cdot 0.3 \cdot b_{\text{y}}(\mathbf{o}_6) \cdot 0.3 \cdot b_{\text{y}}(\mathbf{o}_7) \cdot 0.7 \ \dots$



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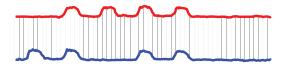
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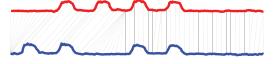
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_Chapitre 8

Dynamic Time Warping (DTW)

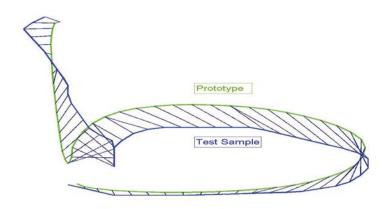
_Chap. 8 DTW: Introduction





Euclidean Distance Sequences are aligned "one to one".

"Warped" Time Axis
Nonlinear alignments are possible.



[M. Sridhar 07]

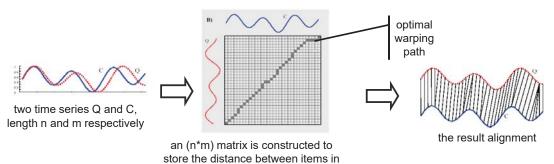


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_Chap. 8 | DTW : Principles

- Principles
 - Given: two sequences C: $x_1, x_2, ..., x_n$ and Q: $y_1, y_2, ..., y_m$
 - Wanted: align two sequences base on a common time-axis



Q and C.

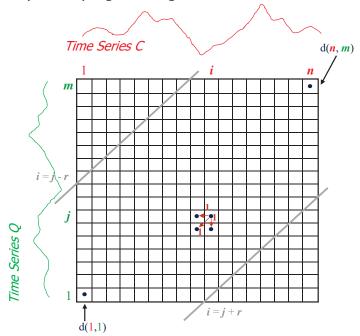
Conditions

- Boundary conditions: We want the path not to skip a part
- Monotonicity: The alignment path does not go back in "time" index
- Continuity: The alignment path does not jump in "time" index
- ... A good alignment path is unlikely to wander too far from the diagonal



_Chap. 8 | DTW : Algorithm

Dynamic programming



$$d(i,j)$$
 = distance between $Q_i \& C_j$ - -for instance $(Q_i - C_j)^2$ $D(i,j)$ = distance cumulée

Initial condition:

$$D(1,1) = d(1,1)$$

$$D(1,j) = \sum_{p=1}^{j} d(1,p) \ j = 1...m$$

$$D(i,1) = \sum_{q=1}^{j} d(q,1)$$
 $i = 1...n$

DP-equation:

$$D(i, j) = min \begin{pmatrix} D(i, j - 1) \\ D(i - 1, j - 1) \\ D(i - 1, j) \end{pmatrix} + d(i, j)$$

Warping window: $j - r \le i \le j + r$.

<u>Time-normalized distance:</u>

$$D(\mathbf{Q}, C) = d(\mathbf{n}, m) / c$$

c = n + m.

The warping path

$$\phi_{qp}(\textbf{k}) = (\phi_{qp}^{q}(\textbf{k}), \phi_{qp}^{p}(\textbf{k}))$$

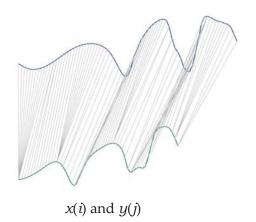
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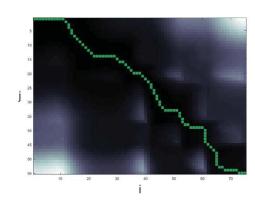
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_Chap. 8 | DTW: Illustration

- Alignment of two pairs of signals
 - The matching between points of two pairs of signals
 - \blacksquare Superimposition of the warping path (ϕ_{xy}) on the cumulative distances matrix D.





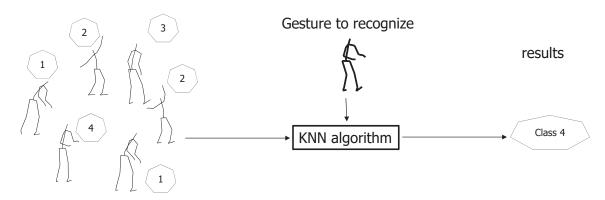
warping path (ϕ_{xy})



[Morel, 2017]

_chap. 8 | DTW : Pattern Recognition using KNN (without learning)

- General Principle:
 - Classification: Distance-based methods
 - → K Nearest-Neighbor Classifier



Gesture samples: One or several samples/class

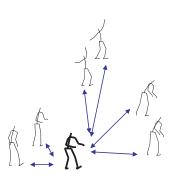


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_chap.8 | DTW : Pattern Recognition using KNN (without learning)

- Basic idea
 - Similarity can be described as distance in a specific space
 - We can use DTW for estimate the distance between tow sequences (gesture)
 - We can use a set of feature for estimate the distance between tow sequences (gesture)
 - If suitable features were selected, that means
 - patterns of the same class have similar features
 - patterns of different classes have dissimilar features
- Need to define
 - ullet A distance function d(x,y) for two arbitrary patterns x and y





_Chap. 8 | DTW: Pattern Recognition using KNN (without learning)

- 1 Nearest-Neighbor Classifier (1NN)
 - Assumption: for each pattern class C_i , $1 \le i \le N$ exactly one (representative) prototype Z_i is given.
 - ullet For an unknown pattern x the following classification rule is then valid:

$$k = \arg\min_{i} \{d(x, Z_i) | 1 \le i \le N\} \Longrightarrow x \in C_k$$

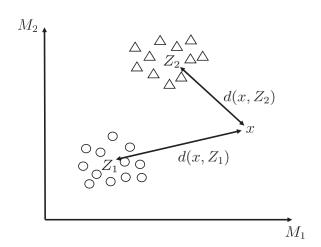
- Task
 - ullet Assign x to the class C_k , to which the next neighbor Z_k in the feature space belongs
 - Reject x , if no unique minimum among $d(x, Z_i)$ exists or if the existing unique minimum is too large
- Nonparametric models
 - requires storing and computing with the entire data set.



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_chap.8 | DTW : Pattern Recognition using KNN (without learning)

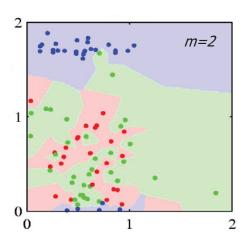
- Nearest-Neighbor Classifier
 - Two pattern classes C_1 and C_2 in the two-dimensional feature space

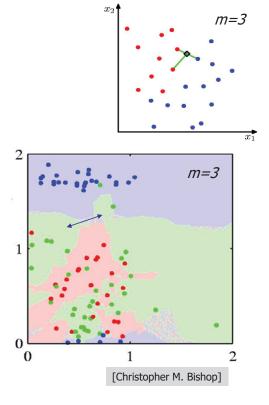




_Chap. 8 | DTW: Pattern Recognition using KNN (without learning)

- k-Nearest-Neighbor Classifier
 - $\begin{tabular}{ll} \bullet & \textbf{Observe the} \ m & \textbf{next neighbors of a pattern} \ x \\ & \textbf{from the sample set.} \\ \end{tabular}$
 - Assign x to the class C_k , which occurs most frequently under all m next neighbors.
 - Common selection $3 \le m \le 7$



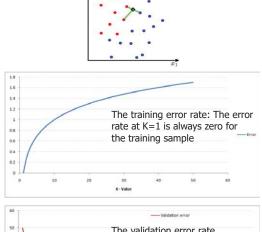


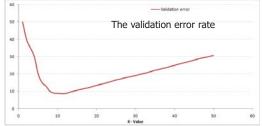


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_chap.8 | DTW : Pattern Recognition using KNN (without learning)

- k-Nearest-Neighbor Classifier
 - How to choose k
 - Common selection $3 \le m \le 7$
- Define K by validation error rate
 - Split the training and validation from the initial dataset.
 - lot the validation error curve to get the optimal value of K.
 - This value of K should be used for all predictions.



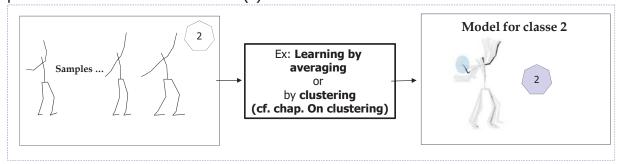




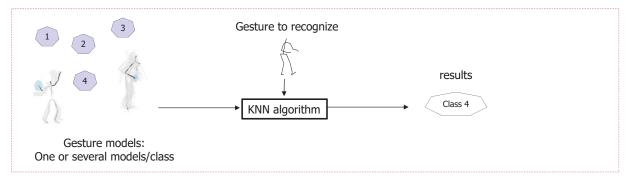
_Chap. 8 | DTW: Pattern Recognition with creating models (Learning phase)

A basic example to learn one or several model(s) for each class

Learning phase for each class



Generalisation phase



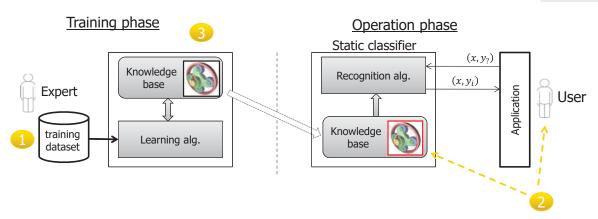


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_chap. 8 | DTW: Pattern Recognition with creating models: Offline learning

[Almaksour 2011]



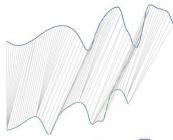
Limitations

- Collecting large and exhaustive training dataset
- User data can be much different from training data (different contexts/habits/needs, time-changing, ...)
- Predefined and fixed set of categories/classes (included in the training dataset)

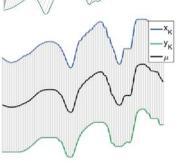


- First idea to average to signals
 - Alignment based on the warping path φxy of length K
 - Creation of two new aligned signals xK (k) and yK(k) with the same length K
 - $xK(k) = x(\phi xxy(k))$

 $yK(k) = y(\phi yxy(k))$



x(i) and y(j)



 $x_{\kappa}(k)$ and $y_{\kappa}(k)$ with the same length K

- \rightarrow result from the resampling of signals x(i) and y(j)relatively to $\varphi_{xy}(k)$
- \rightarrow average signal is $\mu(k)$ (in black).

On drawback: the average signal is longer than the two original signals



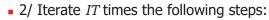
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_Chap. 8 DTW: Averaging of more than two time-series

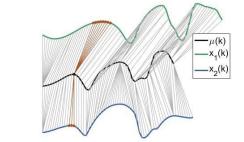
- DTW Barycenter Averaging (DBA) [Petitjean et al. in 2011]
 - A global averaging method for dynamic time warping.
 - A fast algorithm that insures that the average **signal will have a** reasonable length.
- The main steps of the algorithms:
 - 1/ Randomly choose a signal $x_0(k)$ from the dataset to initialize the average signal:

$$\mu(k) = \chi_0(k)$$

$$\mu(k) = x_0(k)$$
, $k = 1, ..., M_0$ where M_0 is the length of $x_0(k)$.



- (a) Align all signals $x_i(k)$ on $\mu(k)$ and compute warping paths $\varphi_{\mu x}$
- (b) Update every point of the average signal $\mu(k)$ as the **barycenter** of points associated to it during step (a).

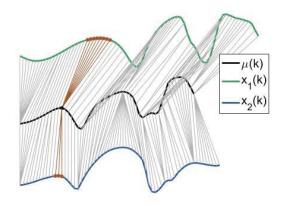


_Chap. 8 | DTW: Barycenter Averaging Algorithm (DBA)

Algorithm 1 DBA: averagingDT W

```
Require: x_0(k) of length M_0, (x_l(k))_{l=1...L} of lengths M_l, IT
   K = M_0, \mu(k) \leftarrow x_0(k), \quad k = 1, ..., K
   for it \in 1...IT do
      assocTab[k] = \emptyset, k = 1...K
      for l \in 1...L do
         \varphi_{\mu x_l} \leftarrow DTW(\mu, x_l)
         p \leftarrow length(\varphi_{\mu x})
         while p \ge 1 do
            (k, n) \leftarrow \varphi_{\mu x}(p)
            assocT ab[k] \leftarrow assocT ab[k] \cup \{x_l(n)\}
            p \leftarrow p - 1
         end while
      end for
      for k \in 1...K do
         \mu(k) \leftarrow mean(assocT \ ab[k])
      end for
   end for
   return \mu(k), k = 1, ..., K
```

[Petitjean *et al.* in 2011] [Morel *et al.* in 2017]



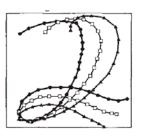


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_chap.8 | DTW: learning category-specific deformations ...

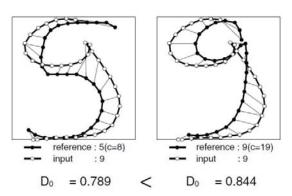
- Problematic
 - Misrecognitions due to overfitting
- Idea
 - To category specific deformations, called eigendeformations, to suppress misrecognitions due to overfitting







[UCHIDA 2005, MOREL 2017]





__Chap. 8 | DTW: learning category-specific deformations ...

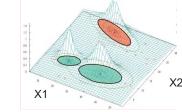
- Some results
 - Estimating deformation tendencies
 - Optimization based on DTW: learning geometric distortions from several examples of the same symbol [UCHIDA 2005]
- NB: Malahanobis Distance
 - Euclidean distance can be re-written as a dotproduct operation

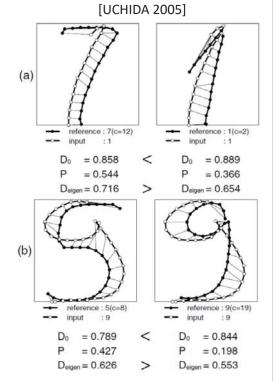
$$d_{L2}(x, y) = \sqrt{(x - y)^T (x - y)}$$

Mahalanobis distance between two vectors, x and

y, where S is the covariance matrix.

$$d_M(x,y) = \sqrt{(x-y)^T S^{-1}(x-y)}$$





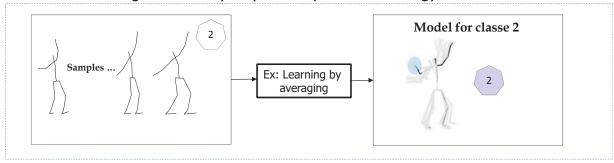
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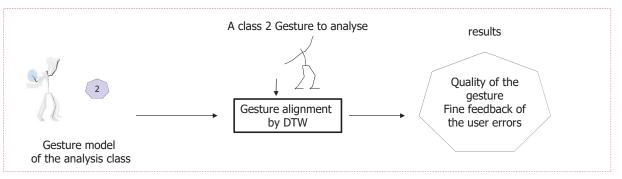
_chap. 8 | DTW : For Gesture Analysis

DTW can also be used for fine gesture analysis (virtual sportive coaching)

Learning phase for each class

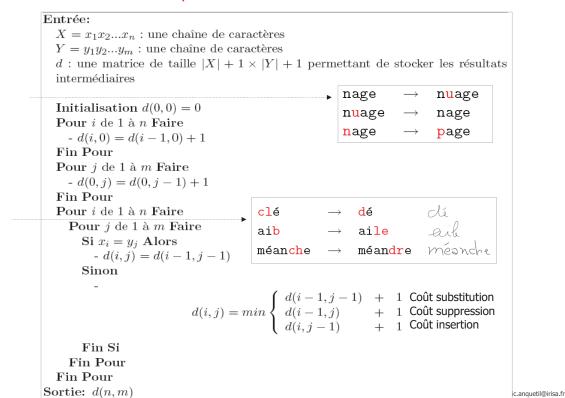


Gesture analysis phase





- Levenshtein distance
 - Insertion
 - Deletion
 - Substitution
- Extension
 - Fusion
 - Division
 - Pair substitution







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Version 1.0

_Chapitre 9

Pre-segmented Action Recognition: Skeleton based and "Statistical" approaches

_chap. 9 | Segmented pattern representation

A pattern refers to either a whole body action or dynamic hand gesture



• The overall process for segmented pattern representation and recognition is:

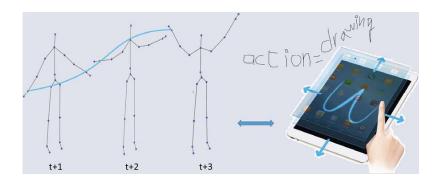




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_Chap. 9 | Skeleton based Action Recognition based on 3D gesture trajectories

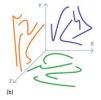
- Addressing 3D action recognition in light of 2D representation
 - 3D gesture trajectories may be processed similarly to hand-drawn trajectories
 - Same data type (trajectories or signal)
 - Graphonomic characteristic:
 - a human is the performer
 - Well-established 2D experience



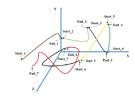


_Chap. 9 | Pre-segmented Action Recognition (Skeleton based)

- Pre-segmented Action Recognition:
 Skeleton based and « statistical » approaches (using SVM)
- Example of two approaches [Boulahia 2017]:
 - A first naïve approach:
 - 3DMM: 3D Multistroke Mapping
 - 3D Multistroke Mapping (3DMM): Transfer of hand-drawn pattern representation for skeleton-based gesture recognition. In 12th IEEE International Conference on Automatic Face & Gesture Recognition (FG 2017), 2017.



- A more robust approach:
 - **HIF3D**: Handwriting-Inspired Features for 3D action recognition
 - HIF3D: Handwriting-Inspired Features for 3D skeleton-based action recognition. In 23rd IEEE International Conference on Pattern Recognition (ICPR), 2016.



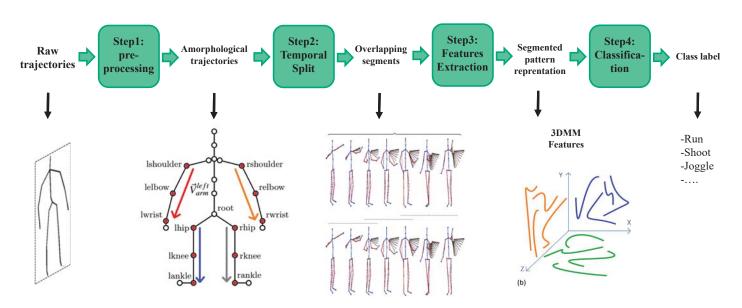


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_chap.9 | Action representation by 3DMM: Kinect based patterns: whole body actions

The overall process for segmented action representation and recognition is:

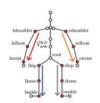




_Chap. 9 | Action representation by 3DMM - Segmented pattern recognition: synthesis

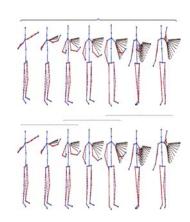
Step 1: Pre-processing

- Goal: address the morphological variability issue
- How: perform a normalisation of the raw trajectories according to the subject morphology



Step 2: Temporal split

- Goal: address the morphological sequencing issue (for instance if two arms are raised at the same time or one after another, the model should distinguish these two different patterns)
- How: Extract partial segments from the whole pattern according to overlapping sliding winodws



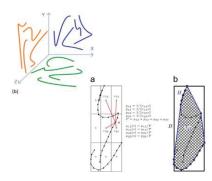


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_chap.9 | Action representation by 3DMM - Segmented pattern recognition: synthesis

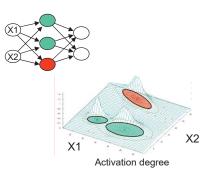
Step 3: Features extraction

- Goal: build the pattern representation that should get the spatial relationship between trajectories and the overall shape of the produced pattern
- How: It consists in extracting a set of features on the whole pattern and on the overlapping segments produced in step 2



Step 4: Classification

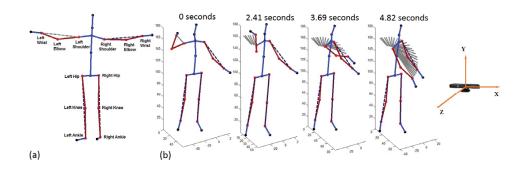
- Goal: get the class label
- How: using a classifier (here SVM or MLP) trained on a training set and then applied on each testing pattern





_chap. 9 | Action representation by 3DMM: Step 1 - Pre-processing

Addressing morphological variability before trajectory extraction



[Kulpa 2005] "Morphology-independent representation of motions for interactive human-like animation", 2005.

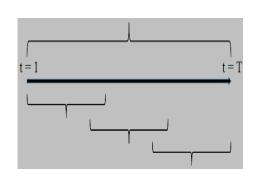


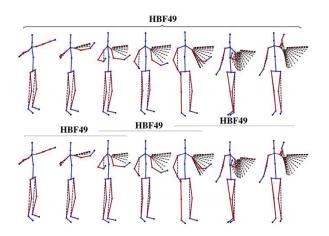
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_chap. 9 | Action representation by 3DMM: Step 2 - temporal hierarchy

- Modelling temporal information: Temporal Split Extraction
 - Handling temporal sequencing
 - Features are extracted according to two temporal levels (Level = 2)
- Number of features:
 - Without selection: 4x49x3=588
 - With selection: between 400 and 80

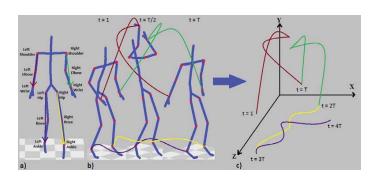


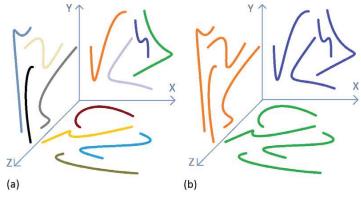




_chap.9 | Action representation by 3DMM: Step 3 - : dealing with the set of 2D trajectories

- A first naïve approach 3DMM using direct 2D projection [Boulahia 2016]
- Several strategies to consider all the trajectories
 - (a) Mono-Stroke approach
 - We loss the spatial dependencies
 - (b) Multi-strokes approach
 - Modelling spatial relationship



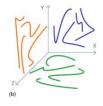




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_chap.9 | Action representation by 3DMM: Step 3 - Direct 2D features extraction

• [Delaye and Anquetil] "HBF49 feature set: A first unified baseline for online symbol recognition", 2013.





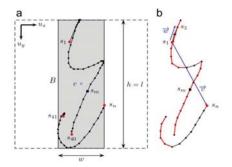


Figure: Descripteurs dynamiques (positions de départ, longueur des strokes, inflexion)

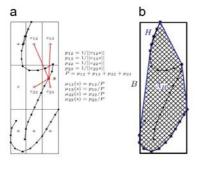
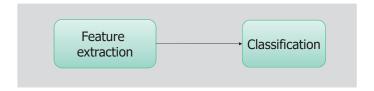


Figure: Descripteurs statiques (histogramme 2D, boite englobante)



_Chap. 9 | Action representation by 3DMM: Step 4 – statistical Learning and classification

Classification



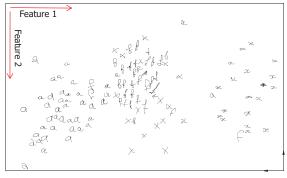
Feature extraction
Discriminative features

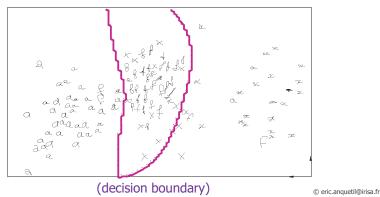
Classification

Use a feature vector to assign the object to a category (class)

Here, 2 dimensions Feature space

Here, discrimination of 3 classes: "a", "f", "x"



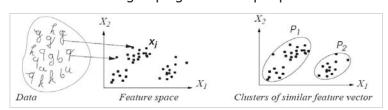


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_Chap. 9 | Action representation by 3DMM: Step 4 – statistical Learning and classification

- Learning
 - Finding all the parameters of a classifier based on a training set.
- Feature extraction Classification

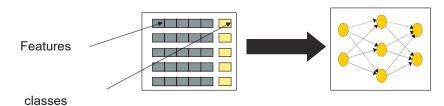
 Learning
- Supervised learning: Generalization
 - For the learning, a teacher provides a category/class label for each pattern in the training set
- Unsupervised learning: Clustering
 - The system forms clusters or "natural groupings" of the input patterns





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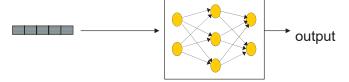
- Learning and generalization capacities
 - Learning
 - consists of presenting an input pattern and modifying the network parameters (weights) to reduce distances between the computed output and the desired output



Input data base

Classifieur

- Generalization / Feedforward
 - consists of presenting a pattern to the input units and passing the signals through the network in order to get outputs units



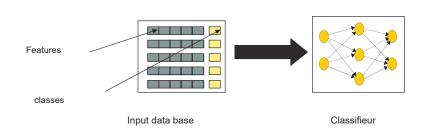


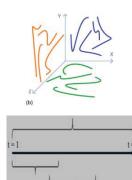
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_Chap. 9 | Action representation by 3DMM: Step 4 – statistical Learning and classification

- Learning: Number of features
 - For each temporal windows: 49 features [HBF 49] x 3 projections = 147
 - 4 temporal windows: the total length of features
 - 588 (147X1 + 147X 3).
 - Feature selection:
 - To limit redundancy
 - between 400 and 80







_chap. 9 | Action representation by 3DMM: Some results on the HDM05 dataset

- HDM05 dataset
 - HDM05 is an optical marker-based dataset
 - M. Müller, T. Röder, M. Clausen, B. Eberhardt, B. Krüger, A. Weber: Documentation Mocap Database HDM05. Technical report, No. CG-2007-2, ISSN 1610-8892, Universität Bonn, June 2007.
 - Contains around 100 motion classes including
 - various walking and kicking motions, cartwheels, jumping jacks, grabbing and depositing motions, squatting motions and so on.
 - Each motion class contains 10 to 50 different instances of the same type of motion
- Experimental Protocol
 - Evaluation with 11 motion actions.
 - The actions are performed by 5 subjects, while each subject performs each action a couple of times;
 - this suggests a set of 249 sequences.
- Testing protocol
 - 3 subjects for learning (142 instances)
 - 2 subjects for testing (109 instances)
 - cross-subjects validation

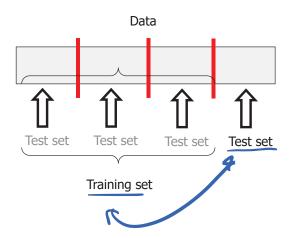


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__Chap. 9 | Evaluation / Validation: Cross-Validation

- Cross-Validation: K-fold
 - Successively setting apart a block of data (instead of a single observation)





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_chap. 9 | Some results of 3DMM approach on the HDM05 dataset

Results (HDM05 dataset)

Method	Authors & Year	#Features	Reco. rate (%)
Dynamic Time Warping MIJA/MIRM + LCSS	[Reyes et al., 2011] [Pazhoumand-Dar et al., 2015]		82.08 85.23
SMIJ + Nearest neighbour	[Ofli et al., 2014]	-	91.53
LDS + SVM	[Chaudhry et al., 2013]	-	91.74
Skeletal Quads + SVM	[Evangelidis et al., 2014]	9360	93.89
Cov3DJ + SVM	[Hussein et al., 2013]	43710	95.41
BIPOD + SVM	[Zhang and Parker, 2015]	-	96.70
HOD + SVM	[Gowayyed et al., 2013]	1116	97.27
3DMM + SVM + Level = 1 3DMM + MLP + Level = 1		100 20	91.74 92.66
3DMM + SVM + Level = 2 3DMM + MLP + Level = 2		400 80	94.49 94.49

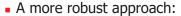
Table: Comparisons between **3DMM** approach, with and without temporal split, and previous approaches on the **HDM05** dataset.



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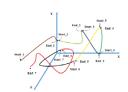
_Chap. 9 | Pre-segmented Action Recognition (Skeleton based)

- Pre-segmented Action Recognition:
 - Skeleton based and « statistical » approaches (using SVM)
- Example of two approaches [Boulahia 2017]:
 - A first naïve approach:
 - **3DMM**: 3D Multistroke Mapping
 - 3D Multistroke Mapping (3DMM): Transfer of hand-drawn pattern representation for skeleton-based gesture recognition. In 12th IEEE International Conference on Automatic Face & Gesture Recognition (FG 2017), 2017.



- **HIF3D**: Handwriting-Inspired Features for 3D action recognition
 - HIF3D: Handwriting-Inspired Features for 3D skeleton-based action recognition. In 23rd IEEE International Conference on Pattern Recognition (ICPR), 2016.



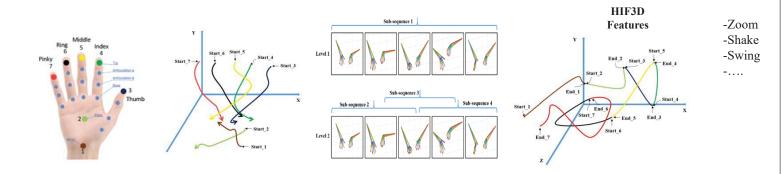




_Chap. 9 | Action representation by HIF 3D: 3D features inspired by 2D features

• The overall process for segmented dynamic hand gesture recognition:







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_Chap. 9 | Action representation by HIF 3D: 3D features inspired by 2D features

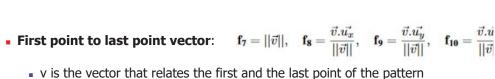
96

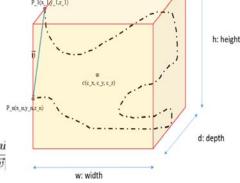
- Overview of the features
 - A new feature-set inspired by an efficient hand-drawn descriptor but entirely dedicated to the 3D skeleton trajectories
 - HIF3D: Handwriting-Inspired Features for 3D skeleton-based action recognition. [Boulahia, ICPR 2016].
 - Extending HBF49 to form HIF3D so as to process directly 3D trajectories instead of projecting
 - Better capturing the correlation between joint trajectories
 - Reducing dimensionality and avoiding redundancy
 - Adding new features (such as volume related features) which are more adapted to 3D patterns
- A set of 89 features (very compact comparing to existing feature-set)
 - 41 Extended features, i.e. features which can directly be extended from 2D trajectory to 3D one.
 - **48 Newly features**, i.e. carry the characteristic information identified for handwritten pattern but have different formulations since the original 2D formulas can not be directly applied for the 3D case.



Extended features:

- **Starting** points: $\mathbf{f_1} = \frac{x_1 c_x}{l} + \frac{1}{2}$, $\mathbf{f_2} = \frac{y_1 c_y}{l} + \frac{1}{2}$, $\mathbf{f_3} = \frac{z_1 c_z}{l} + \frac{1}{2}$
 - x1, y1 and z1 are the coordinates of the first point of the pattern
 - cx, cy and cz are the coordinates of the the center of the bounding box B
 - I is the greatest side of the bounding box B
 - The bounding box B is the cuboid that enclose the pattern





- Bounding box diagonal angles: $f_{21} = \arctan\left(\frac{h}{w}\right)$, $f_{22} = \arctan\left(\frac{d}{h}\right)$, $f_{23} = \arctan\left(\frac{w}{d}\right)$
 - h, w and d are the height, the width and the depth of the bounding box B, respectively.



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_chap.9 | Action representation by HIF 3D: 3D features inspired by 2D features

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- Newly features:
 - 3D zoning histogram:
 - $\,\blacksquare\,$ We define a regular 3D partition of the bounding box B into 3 $\times 3 \times 3$ voxels resulting in twenty-seven zoning features
 - Histograms are built by computing a fuzzy weighted contribution from each point si
 to its eight neighbouring voxels, where the weights are proportional to the distance
 from the point to the voxels center cj,k,l.

$$\mathbf{f_{58}} = \frac{1}{n} \sum_{i=1}^{n} \mu_{111}(s_i), \dots \mathbf{f_{84}} = \frac{1}{n} \sum_{i=1}^{n} \mu_{333}(s_i)$$

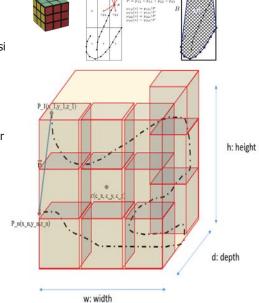
• With $0 \le \mu$ jkl(si) ≤ 1 is the contribution of point si to the voxel with center c j,k,l for each $1 \le j,k,l \le 3$

Convex Hull features:

- To capture the overall shape produced during the gesture we consider the convex hull H of the resulting pattern S
- We first compute its convex hull volume VH.
- Then we extract the normalized volume and the compactness as two additional features

$$\mathbf{f_{88}} = rac{V_H}{\mathbf{w} * \mathbf{h} * \mathbf{d}}, \qquad \mathbf{f_{89}} = rac{L^3}{V_H}$$

 L is the total length of the pattern and w, h and d are the height, the width and the depth of the bounding box B, respectively



_Chap. 9 | Some results of HIF3D approach on the HDM05 dataset

Experimental Protocol: 3 subjects for learning (142 instances) + 2 subjects for testing (109 instances)

Method	Authors & Year	#Features	Reco. rate (%)
Dynamic Time Warping MIJA/MIRM + LCSS	[Reyes et al., 2011] [Pazhoumand-Dar et al., 2015]	- -	82.08 85.23
SMIJ + Nearest neighbour	[Ofli et al., 2014]	-	91.53
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BIPOD + SVM	[Zhang and Parker, 2015]	-	96.70
HOD + SVM	[Gowayyed et al., 2013]	1116	97.27
3DMM + SVM + Level = 2		400	94.49
HIF3D + SVM + Level = 2		356	98.17



Table: Comparisons between **HIF3D** approach, with temporal split, and previous approaches on the HDM05 dataset.



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_Chapitre 10

Non-segmented Action Recognition: Skeleton based and "Statistical" approaches

chap. 10 | 2D and 3D Action/Gesture recognition: a challenge?

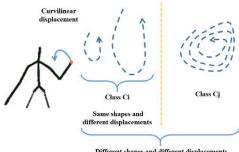
- Introduction: understand the problematic of gesture interaction
 - What is a gesture: the different natures of gestures
 - Human Computer Interaction: new opportunities
- Gesture recognition: Isolated Gestures Classification (segmented)
 - Overview of the task: recognizing isolated gestures (The overall pattern recognition process)
 - Machine Learning and Pattern recognition: a short overview of some existing techniques
 - Gesture classication: "Time-series" approaches
 - Pre-segmented Action Recognition: Skeleton based and "Statistical" approaches
- Gesture recognition in real-time streaming (non segmented)
 - Overview of the task: recognizing in real-time streaming
 - Non-segmented Action Recognition: Example of one approaches [Boulahia 2017]
 - Presentation of experimental results using Kinect and Leap Motion
- Early Gesture recognition

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_Chap. 10 | Gesture recognition in real-time streaming (non segmented): overview

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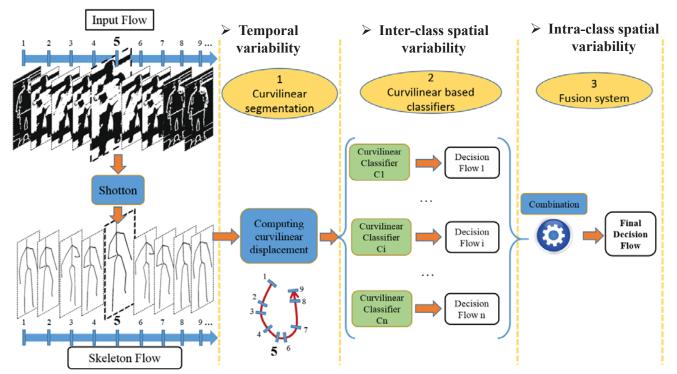
- The challenges that should be addressed are:
 - Temporal variability: that occurs when subjects perform gestures with different speeds.*
 - Inter-class spatial variability: which refers to disparities between the displacement amounts induced by different classes (i.e. long vs. short movements).
 - Intra-class spatial variability: caused by differences in style and gesture amplitude.



Different shapes and different displacements



_Chap. 10 | Gesture recognition in real-time streaming (non segmented): overview





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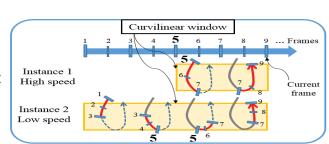
__Chap. 10 | Gesture recognition in real-time streaming (non segmented): step 1

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- Step 1: curvilinear segmentation
 - Dynamically defining windows depending on the amount of information (i.e. motion) available in the unsegmented flow.
 - The metric used to measure the amount of information is the curvilinear displacement of joints.
 - function CuDi(FS,FE) that computes the curvilinear displacement for a given motion segment, starting at frame FS and ending at FE, as follows:

$$CuDi(F_S, F_E) = \sum_{i=F_S}^{i=F_E} d_i^{Avg}$$

where d_i^{Avg} is the instantaneous average displacement



- Curvilinear window as being a sliding window
 - whose size is continuously updated such that it encompasses, at each frame, a specific curvilinear displacement.



_Chap. 10 | Gesture recognition in real-time streaming (non segmented): step1

Step 1: curvilinear segmentation

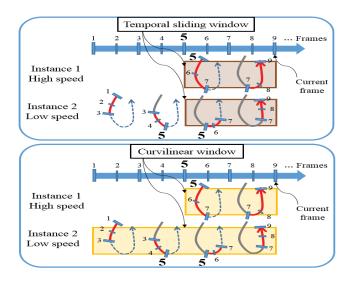
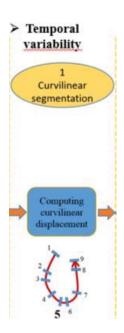


Illustration of the difference between the curvilinear window and the usual temporal sliding window.





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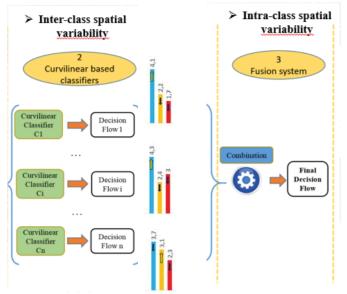
_chap. 10 | Gesture recognition in real-time streaming (non segmented): step 2

- Step 2: curvilinear-based classifiers
 - To address the second issue, inter-class spatial variability, we propose to use as many classifiers as there are curvilinear displacements.
 - Each classifier Ci is trained to recognize all action classes but according to the curvilinear size of classe Gi
 - We constitute the training set of a classifier Ci by extracting local features (HIF3D) according to its corresponding curvilinear window.
 - **SVM** classifiers are then trained on each training set.

➤ Inter-class spatial variability Curvilinear based classifiers Curvilinear Decision Classifier Flow 1 CI Curvilinear Decision Classifier Flow i Ci Curvilinear Decision Classifier Flow n Cn

Step 3: Decision process (at each frame)

- The fusion system is mainly composed of:
 - as many **local histograms** as there are classifiers && a **global histogram**



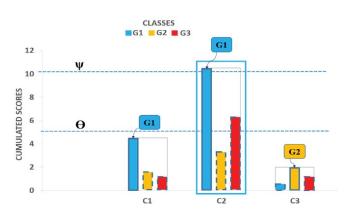


Illustration of the **global histogram** functioning at frame i with three classifiers which can G1, G2 or G3

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_chap. 10 | Gesture recognition in real-time streaming (non segmented): step 3

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Step 3: Decision process

- Each local histogram has as many entries as there are classes to predict.
 - It is used to cumulate (at each frame) the score of each class predicted by the associated classifier Ci.
- Then, at each instant, each local histogram is updated
- the jth entry of a histogram $llis_i$ associated with classifier ℓi is updated at each instant:
 - β equals to the difference between
 - the score of the currently predicted class, i.e. Predicted_i,
 - and the score of the secondly ranked predicted class by the classifier (i.
 - γ corresponds to the difference between
 - the score of Predicted_i
 - and that of jth class corresponding to the jth entry of the histogram.

$$His_i(j) = \begin{cases} His_i(j) + \beta, & \text{if } j = Predicted_i \\ His_i(j) - \gamma, & \text{otherwise} \end{cases}$$

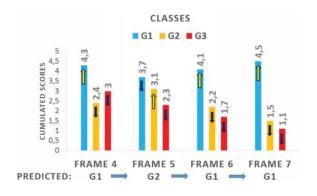
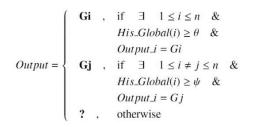


Illustration of a **local histogram** functioning with three classes at frames 4, 5, 6 and 7



- Step 3: Decision process
 - Then, at each instant, each local histogram is used to update the global histogram.
 - This latter is responsible for emitting the final decision.
 - At each decision, all histograms are reinitialized to zeros, as are the cumulated curvilinear displacements for each classifier.



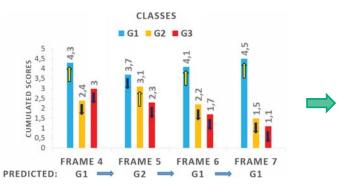


Illustration of a **local histogram** functioning with three classes at frames 4, 5, 6 and 7

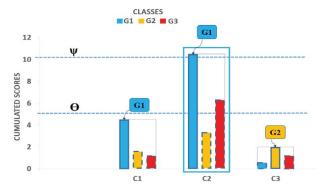


Illustration of the **global histogram** functioning at frame 7 with three classifiers which can G1, G2 or G3



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_Chapitre 11

Presentation of experimental results using Kinect and Leap Motion

DataSet: MSRC-12 dataset

- The Microsoft Research Cambridge-12 dataset (MSRC-12): sequences of skeleton data, represented as 20 joint locations.
 - S. Fothergill, H. Mentis, P. Kohli, S. Nowozin, Instructing people for training gestural interactive systems, in: Proceedings of the SIGCHI Conference on Human Factors in Computing Systems, ACM, pp. 1737–1746.
 - 12 gestures performed by 30 subjects
 - **594** seguences (about 50 seguences per class)
 - a single gesture is performed several times along a sequence.
- Participants were provided with 5 instruction modalities including:
 - images, text, video, images + text, and video + text.
- The dataset is annotated with action points
 - a pose within the gesture that clearly identifies its completion.

Metaphoric gestures	Main frames	Iconic gestures	Main frames
Start music\ raise volume (G1)		Crouch or hide(G2)	1 中
Navigate to next menu(G3)		Put on night vision googles(G4)	1
Wind up the music(G5)	个个工作个	Shoot with a pistol(G6)	
Take a bow to end the session(G7)	九九九	Throw an ob- ject such as a grenade(G8)	有并为
Protest the music(G9)		Change weapon(G10)	À À
Lay down the tempo of a song(G11)	7444	Kick to at- tack an en- emy(G12)	17

[Xi Chen, Markus Koskela 2015]

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Chap. 11 Gesture recognition in real-time streaming (non segmented): MSRC-12 Dataset

- Protocol (MSRC-12 dataset)
 - According to the leave-subjects-out protocol.
 - Mean F_{score} and its standard deviation is reported for each instruction modality.
- Other approaches
 - ELS = Efficient Linear Search:
 - RF = Random Forests:
 - RTMS = Real-Time Multi-Scale;
 - SSS =Structured Streaming Skeleton.
 - CuDi3D [Boulahia 2017]

	ELS [12]	RF [3]	RTMS [11]	SSS [4]	ELS [13]	CuDi3D
Video - Text	0.645 ± 0.149	0.679 ± 0.035	0.713 ± 0.105	0.707 ± 0.170	0.790 ± 0.133	0.848 ± 0.060
Images - Text	0.581 ± 0.134	0.563 ± 0.045	0.656 ± 0.122	0.730 ± 0.148	0.711 ± 0.228	0.744 ± 0.072
Text	0.437 ± 0.170	0.479 ± 0.104	0.521 ± 0.072	0.713 ± 0.191	0.622 ± 0.246	0.695 ± 0.080
Video	0.580 ± 0.189	0.627 ± 0.052	0.635 ± 0.075	0.557 ± 0.291	0.726 ± 0.225	0.816 ± 0.060
Images	0.497 ± 0.122	0.549 ± 0.102	0.596 ± 0.103	0.666 ± 0.194	0.670 ± 0.254	0.719 ± 0.087
Overall	0.548	0.579	0.624	0.675	0.704	0.764



Precision * Recall

 $F_{score} = 2 * \frac{Freeson.}{Precision + Recall}$

Chap. 11 | Evaluation measure

Evaluation measure

		Desired Pos	sitive	Desired Negative	
	Positive N _E	True Positive	N_E^A	False Positive	N_R^A
Test Outcome	Negative N _R	False negative	N_E^R	True Negative	N_R^R

Recognition/Error Rates

TAR: True Acceptance RateFAR: False Acceptance Rate

$$TAR = \frac{N_E^A}{N_E}$$

$$FAR = \frac{N_R^A}{N_R} \bigg| \bigg\rangle$$

Accuracy Rates ("fiabilité")

Global performance point of view

 $Accuracy = \frac{N_E^A + N_R^R}{N_E + N_R}$

recall ("rappel")

information retrieval → the number of relevant documents retrieved by a search / the total number of existing relevant documents

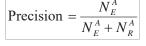
Recall = TAR

Precision ("précision")

the number of items correctly labeled ∈the positive class / the total number of elements labeled ∈ the positive class

 information retrieval → number of relevant documents retrieved by a search divided by the total number of documents retrieved by that search

 The <u>F-Score</u> (or F Measure) conveys the balance between the precision and the recall.



$$F_{score} = 2 * \frac{Precision * Recall}{Precision + Recall}$$



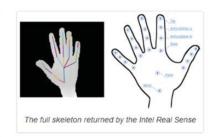
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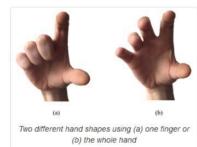
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_Chap. 11 | Gesture recognition in real-time streaming / segmented: (DHG) dataset

- DHG DATASET: Dynamic Hand Gesture
 - DHG is a recent dynamic hand gesture dataset
 - [De Smedt 2016] Quentin De Smedt, Hazem Wannous, and Jean-Philippe Vandeborre. Skeleton-based dynamic hand gesture recognition. In Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition Workshops, pages 1–9, 2016.
 - 14 pre-segmented hand gestures
 - performed in two ways: using one finger and the whole hand.
 - Each gesture is performed between 1 and 10 times by **28 participants**
 - in 2 ways (one finger / the whole hand)
 - resulting in 2800 instances.
 - Each frame of sequences contains
 - a depth image
 - the **coordinates** of 22 joints both in the 2D depth image space and in the 3D world space forming a **full hand skeleton**.







_Chap. 11 | Gesture recognition in real-time streaming / segmented: (DHG) dataset

- DHG: Segmented Gesture recognition in real-time streaming
 - COMPARISON BETWEEN
 - [Boulahia 2017] HIF 3D APPROACH
 - AND PREVIOUS APPROACHES
 - CONSIDERING 14 AND 28 GESTURES ON DHG* DATASET

Method	14 gestures (%)	28 gestures (%)
HoWR [3]	35.61	-
SoCJ [3]	63.29	-
HoHD [3]	67.64	-
Oreifej and Liu [12, 14]	78.53	74.03
Devanne et al. [5, 14]	79.61	62.00
SoCJ + HoHD [3]	82.29	-
Guerry <i>et al</i> . [14]	82.90	71.90
SoCJ + HoHD + HoWR [3]	83.07	80.00
Ohn-Bar and Trivedi [11, 14]	83.85	76.53
De Smedt et al. [3, 14]	88.24	81.90
Our	90.48	80.48

[SHREC 2017] Results of the SHREC 2017 challenge on dynamic hand gesture recognition [Boulahia,IPTA 2017] Dynamic hand gesture recognition based on 3D pattern assembled trajectories. In 7th IEEE International Conference on Image Processing Theory, Tools and Applications (IPTA 2017).



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_chap. 11 | Gesture recognition in real-time streaming / segmented: (DHG) dataset

CONFUSION MATRIX USING 14 GESTURES OF DHG DATASET

G 87.9 3.4 0.0 5.2 1.7 0.0 0.0 0.0 0.0 1.7 0.0 0.0 0.0 0.0 11.5 63.9 9.8 1.6 1.6 3.3 0.0 0.0 0.0 4.9 0.0 0.0 3.3 0.0 P 1.8 1.8 94.5 0.0 0.0 0.0 0.0 0.0 1.8 0.0 0.0 0.0 0.0 0.0 R-CW 13.7 2.0 0.0 82.4 0.0 0.0 2.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 R-CCW 89.1 5.5 1.8 1.8 0.0 0.0 1.8 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 T 3.4 0.0 0.0 0.0 0.0 91.4 5.2 0.0 0.0 0.0 0.0 0.0 0.0 S-R 0.0 0.0 0.0 1.6 0.0 98.4 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 94.4 0.0 0.0 S-L 0.0 0.0 0.0 1.9 3.7 0.0 0.0 0.0 0.0 0.0 S-U 0.0 1.5 11.8 0.0 0.0 1.5 0.0 0.0 83.8 1.5 0.0 0.0 0.0 S-D 0.0 1.6 0.0 9.8 0.0 0.0 0.0 0.0 0.0 86.9 0.0 0.0 1.6 0.0 98.6 S-X 0.0 0.0 0.0 0.0 0.0 0.0 0.0 1.4 0.0 0.0 0.0 0.0 0.0 S-V 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 1.8 98.2 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 1.7 0.0 0.0 98.3 0.0 S-+ 0.0 0.0 2.7 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 Sh 0.0 0.0 0.0 97.3 P.CN 0 3

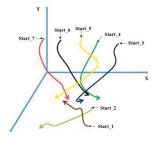


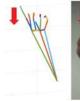
- Weaknesses of existing dynamic hand gesture datasets:
 - Composed of very short clips (around 30 frames)
 - Gestures are performed with a single hand
 - Perfectly denoised, with almost no missing motion segments
 - Composed of pre-segmenetd gestures only

LMDHG dataset:

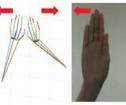
A leapMotion (NON-) Segmented DataSet













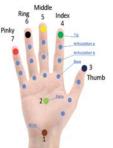


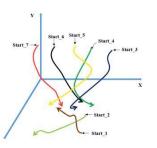
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_Chap. 11 | Gesture recognition in real-time streaming / NON-segmented: (LMDHG) dataset 118

- LMDHG dataset: A leapMotion DataSet
 - Composed of 50 unsegmented sequences of gestures performed with either one hand or both hands by 21 participants
 - Each sequence contains 13 ± 1 class gestures leading to a total of 608 gesture instances
 - Order of class in each sequence is aleatory
 - Each frame contains the 3D coordinates of 46 joints
 - Ground truth Start/End along with the class labels are provided
 - LMDHG dataset contains noisy and incomplete gestures.









Gesture	#Hands	tag name
Point to	1	HG1
Catch	1	HG2
Shake with two hands	2	HG3
Catch with two hands	2	HG4
Shake down	1	HG5
Shake	1	HG6
Draw C	1	HG7
Point to with two hands	2	HG8
Zoom	2	HG9
Scroll	1	HG10
Draw Line	1	HG11
Slice	1	HG12
Rotate	1	HG13



- CONFUSION MATRIX ON THE COLLECTED LMDHG DATASET
 - [Boulahia, IPTA 2017] Dynamic hand gesture recognition based on 3D pattern assembled trajectories. In 7th IEEE International Conference on Image Processing Theory, Tools and Applications (IPTA 2017).
 - **Protocol**: train on 70% of the sequences,
 - Train i.e. sequences from 1 to 35
 - Test on the remaining 15 sequences.
 - Overall score:
 - **Segmented**: 84.78%

HG1	92.9	7.1	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
HG2	6.7	80.0	0.0	6.7	6.7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
HG3	0.0	0.0	92.9	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	7.1
HG4	0.0	6.7	0.0	86.7	0.0	0.0	0.0	0.0	6.7	0.0	0.0	0.0	0.0
HG5	0.0	6.7	0.0	0.0	66.7	0.0	0.0	0.0	0.0	0.0	0.0	20.0	6.7
HG6	0.0	0.0	0.0	0.0	0.0	85.7	0.0	0.0	0.0	0.0	7.1	0.0	7.1
HG7	0.0	0.0	6.7	0.0	0.0	0.0	93.3	0.0	0.0	0.0	0.0	0.0	0.0
HG8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	100.0	0.0	0.0	0.0	0.0	0.0
HG9	0.0	0.0	0.0	0.0	0.0	0.0	8.3	0.0	83.3	0.0	0.0	0.0	8.3
HG10	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	92.9	0.0	0.0	7.1
HG11	0.0	6.7	6.7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	86.7	0.0	0.0
HG12	0.0	6.7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	6.7	0.0	86.7	0.0
HG13	0.0	0.0	6.7	0.0	6.7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	86.7
	HG1	HG2	HG3	HG4	HG5	HG6	HG7	HG8	HG9	HG10	HG11	HG12	HG13



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_Chap. 11 | Gesture recognition in real-time streaming / NON-segmented: (LMDHG) dataset 120

- Experimental results on LMDHG dataset : Unsegmented gestures
 - BaseLine with a basic approach
 - A sliding window approach in which the window size equals to the average of training instances
 - Protocol
 - train on 70% of the sequences, i.e. sequences from 1 to 35
 - test on the remaining 15 sequences.
 - For evaluating this basic approach with unsegmented sequences, we use the Fscore :
 - Overall Fscore: 54.11%

$$F_{score} = 2 * \frac{Precision * Recall}{Precision + Recall}$$





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_Chapitre 12 Early Recognition

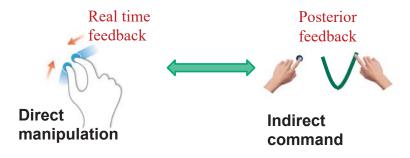
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_Chap. 12 | 2D and 3D Action/Gesture recognition: a challenge?

- Introduction: understand the problematic of gesture interaction
 - What is a gesture: the different natures of gestures
 - Human Computer Interaction: new opportunities
- Gesture recognition: Isolated Gestures Classification (segmented)
 - Overview of the task: recognizing isolated gestures (The overall pattern recognition process)
 - Machine Learning and Pattern recognition: a short overview of some existing techniques
 - Gesture classication: "Time-series" approaches
 - Pre-segmented Action Recognition: Skeleton based and "Statistical" approaches
- Gesture recognition in real-time streaming (non segmented)
 - Overview of the task: recognizing in real-time streaming
 - Non-segmented Action Recognition: Example of one approache [Boulahia 2017]
 - Presentation of experimental results using Kinect and Leap Motion
- Early Gesture recognition

__Chap. 12 | Gesture Early Recognition: Introduction

- One possible Goal for Early recognition:
 - To merge **Direct** and **Indirect** interactions into a same interface
 - we have to distinguish gesture in the very beginning part



- One Solution:
 - a reject option based multi-classifier system
 - for handwritten gesture early recognition [Zhaoxin 2016]



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Gesture B

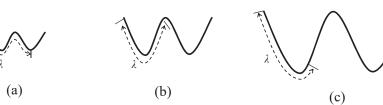
Gesture C

_chap. 12 | Gesture Early Recognition: Difficulties for Recognition

- Goal: recognize the gesture
 - from their early part
 - instead of waiting until the end of them.

Difficulties

- to deal with the common beginning part ambiguity
- The proportion of the earliness is unpredictable
 - (a) A normalized gesture as a template.
 - (b) (c) In a size free context.





Common part

Gesture A

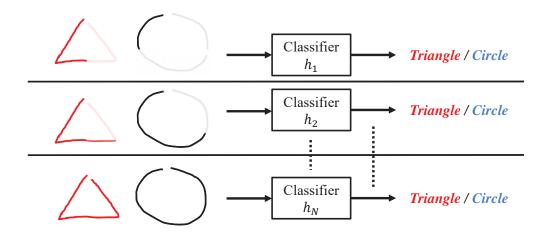
Common part



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__Chap. 12 | Gesture Early Recognition: A multi-classifier early recognition system

 During the training, each classifier dedicates to different part of gestures (short, medium, long)



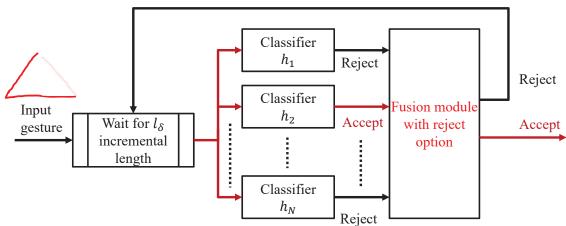


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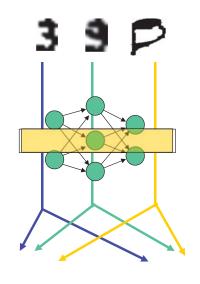
_chap. 12 | Gesture Early Recognition: Reject option

- One strategy: A reject option based multi-classifier early recognition system
 - All classifiers try to recognize the gestures
 - The fusion module merge trustable decisions
- Two types of reject are used to evaluate the confidence
 - ambiguity: the shape looks like beginning of several different gesture classes
 - outlier: the classifier has never seen this type of shape



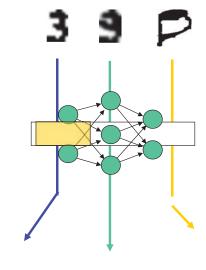


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Good recognition

Confusion



Good recognition

Confusion Reject Distance Reject

Unknown input

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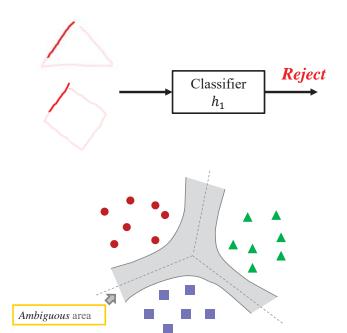
_chap. 12 | Gesture Early Recognition: Ambiguity rejection

Ambiguity rejection [5]

$$\psi_i^{Amb} = \frac{p_i - p_j}{p_i}$$

where p_i is the confidence value of best class, p_j is the second best class from the classifier.

[5] H. Mouchère and E. Anquetil. **A unified** strategy to deal with different natures of reject. In Pattern Recognition, 2006. ICPR 2006, volume 2, pages 792-795, 2006.





Outlier rejection

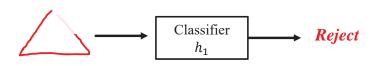
Estimate the outlier confidence value using the minimum distance to the prototypes:

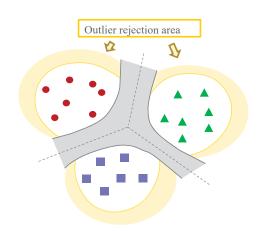
$$D_i = \min_{j \in N} (d(g_t, g_i^j))$$

 g_t is a test sample, g_i is the prototype sample of class i, N is the number of prototypes.

Reliability function

$$\psi_i^{Out} = \begin{cases} e^{-\frac{(D_i - \mu)}{2\sigma^2}} & \text{if } D_i \ge \mu \\ 1 & \text{if } D_i < \mu \end{cases}$$





Where μ and σ is the minimum distance and deviation computed from validation set.

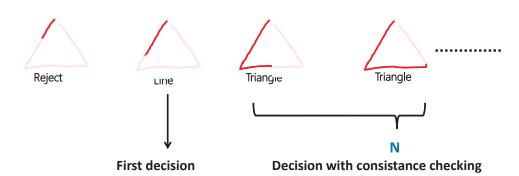


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_chap. 12 | Gesture Early Recognition: consistance checking

- Dynamic decision with consistance checking (N)
 - N consecutive identical results in the stream of outputs
 - Several recognitions during the drawing with more and more information



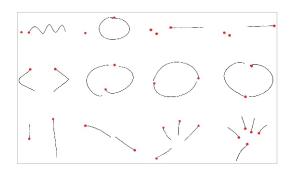


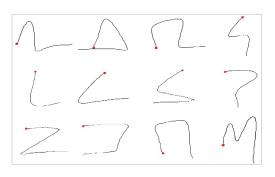
_Chap. 12 | Gesture Early Recognition: Experiments

Examples of Gestures: MGSet/ILG datasets

- (MGSet) Multi-stroke gestures (45 classes, 33 users, 6K samples)
- (ILG) Single-stroke gestures (45 classes, 21 users, 2K samples)









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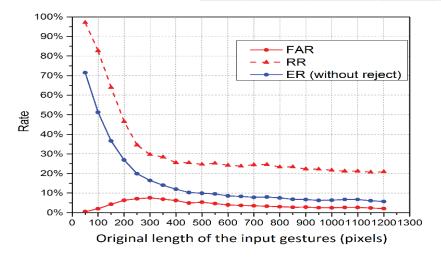
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_chap. 12 | Gesture Early Recognition: Experiments

Results (MGSet)

- (MGSet) Multi-stroke gestures
 (45 classes, 33 users, 6K samples)
- Results with decision consistence:
 reject opt. allows to improve earliness

N	With Reject Option (MGSet)									
IN	TAR	FAR	RR	Earliness	Avg. T (ms)					
1	81.89%	14.56%	3.54%	37.04%	456.21					
2	83.44%	10.85%	5.71%	46.82%	523.34					
3	82.38%	8.85%	8.77%	55.89%	591.33					







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_Chapitre 13 Fuzzy Clustering

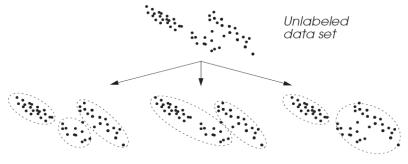
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_Chap. 13 | Fuzzy clustering: Introduction

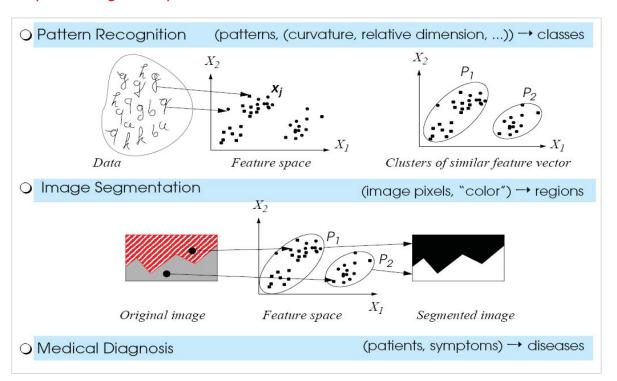
• What is cluster analysis?

"partitioning a collection of data points into a number of subgroups (clusters), where the objects inside a cluster show a certain degree of closeness or similarity"



- Major difficulties to find "natural groupings":
- √ Large variability in cluster shapes
 - Classification criterion Similarity or distance measure
- ✓ Number of clusters ?
 - Cluster validity problem







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_Chap. 13 | Fuzzy clustering: Outline

- 1. Data Representation and Notation
 - Features
 - Partitions
- 2. Clustering Methods
 - Different clustering families
 - Principles of alternating optimization
 - Hard C-Means
 - Fuzzy C-Means
 - Possibilistic Clustering
 - Cluster Validity
- 3. Discussion and Application



Notation

- let $D = \{x_i / j = 1 ... N\}$ be the data set of N items x_i
- let $P = \{ P_i / i = 1...C \}$ be the C cluster prototypes
- Each x_i is described by a feature vector: $x_i = (x_{i1}, x_{i2}, ..., x_{in})^T$

(Data , Feature space)
$$\rightarrow$$
 clusters $(x_j, x_j = (x_{j1}, x_{j2}, \dots, x_{jn})^T) \rightarrow P_i$

O C-Partition

• A C-partition can be represented by a (CxN) matrix $U=(\mu_{ij})$, where μ_{ij} represents membership of \mathbf{x}_j in \mathbf{P}_i

data points

$$\mathbf{U} = \text{Clusters} \begin{bmatrix} \mu_{11} \hdots \mu_{1j} \hdots \mu_{1N} \\ \hdots \hdot$$

 A clustering algorithm = finds the { U_{HCM}, U_{FCM}, U_{PCM}} which "best" explains and represent the structure in X.



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_chap. 13 | Fuzzy clustering: Data Representation

- Different partition properties

$$\mathsf{U}_{\mathsf{HCM}} = \ \mu_{ij} \in \{0,1\} \; , \; 0 < \sum_{j \; = \; l}^{N} \mu_{ij} < N \; , \; \sum_{i \; = \; l}^{C} \mu_{ij} \; = \; 1$$

constrained fuzzy partition:

$$\mathsf{U}_{\mathsf{FCM}} = \left[\mu_{ij} \in [0,1] \right], \ 0 < \sum_{j=1}^{N} \mu_{ij} < N \ , \ \sum_{i=1}^{C} \mu_{ij} = 1$$

•• unconstrained fuzzy partition: $U_{PCM} = \sum_{i=1}^{C} \mu_{ij} = 1$

do not necessarily sum up to one over any column

$$U_{HCM} \subset U_{FCM} \subset U_{PCM}$$



Probabilistic Clustering

Example: Gaussian mixture decomposition

Competitive Learning
 Neural network based algorithms

Example: Self Organization Map (SOM)

Vector Quantization

Example: LBG algorithm

Alternating optimization
 Clustering methods based on objective function

Example: Fuzzy C-Means algorithm

>> Many common points between these different approaches <<



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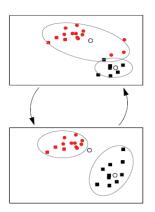
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_Chap. 13 | Fuzzy clustering: Alternating Clustering methods

General principle

"Alternating clustering methods are based on an iterative minimization of a criterion function (objective function) to extract a partition of the data set"

- General iterative algorithm / alternating optimization
 - √ step 1 (Initialization)
 - ullet Fix ${m C}$, initial ${m C} ext{-partition}$, ...
 - √ step 2 (Prototype adaptation)
 - ullet Calculate the C prototypes $extbf{\emph{P}}_{ extbf{\emph{i}}}$
 - √ step 3 (Update the C-partition)
 - "Label" evaluation of the data
 - Update the C-partition matrix **U**
 - √ step 4 (Termination)
 - Repeat steps 2-4 until the termination criterion is met





Based on a constrained crisp partition:

$$\mu_{ij} \in \{0,1\}$$
, $0 < \sum_{j=1}^{N} \mu_{ij} < N$, $\sum_{i=1}^{C} \mu_{ij} = 1$

➡ The Objective function is the WGSS:

$$J_{P, U, D} = \sum_{i=1}^{C} \sum_{x_j \in P_i} d^2(x_j, P_i)$$

OHCM algorithm (Duda and Hart (Dud73))

√ step 1 (Initialization)

• **Fix** 2 ≤ **C** < **N**, initial **C-partition U**(0)

√ step 2 (Prototype adaptation)

ullet Calculate the C prototypes P_i

√ step 3 (Update the C-partition)

• Update the C-partition matrix **U**(t)

√ step 4 (Termination)

• Repeat steps 2-4 until ΔU < ε

$$P_{i} = \frac{\sum_{j=1}^{N} \mu_{ij}^{x_{j}}}{\sum_{j=1}^{N} \mu_{ij}}$$

$$\mu_{ij}(t+1) = \begin{cases} 1, \ d(x_j, P_i(t)) = \min_{1 \le k \le C} (d(x_j, P_k(t))) \\ 0, \text{ otherwise} \end{cases}$$



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_chap. 13 | Fuzzy clustering: Constrained crisp partition

- $\mu_{ij} \in \{0,1\}$, $\sum_{i=1}^{C} \mu_{ij} = 1$: means that each \mathbf{x}_{i} is in exactly one of the C clusters.
- $0 < \sum_{j=1}^{N} \mu_{ij} < N$: means that no cluster is empty and no cluster is all of X.
- The objective function is the classical WGSS (Within Group Sum of Squared errors)

$$J_{P, U, D} = \sum_{i=1}^{C} \sum_{j=1}^{N} \mu_{ij} d^{2}(x_{j}, P_{i})$$

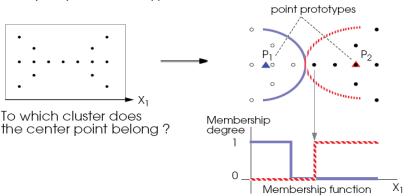
where \mathbf{d}^2 represents a distance measure, for example the euclidean distance measure:

$$d^{2}(x_{j}, P_{i}) = ||x_{j} - P_{i}||^{2} = \sum_{k=1}^{n} (x_{jk} - P_{ik})^{2}$$

The second version is based on: find the centroid → reallocate the cluster memberships to minimize the errors between the data and the prototypes.

$$P(\uparrow -1) \rightarrow U(\uparrow) \rightarrow P(\uparrow)$$

Classical example (The butterfly)



- Discussion
 - ➡ In HCM clustering every point belongs to only 1 cluster (constrained crisp partition)
 - Transition between full membership and no membership is abrupt
 - → Hard decisions on class assignments
 - ➡ Consequently the 2 clusters can not be symmetric with respect to the center point



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_chap. 13 | Fuzzy clustering: Fuzzy C-Means

■ Based on a constrained fuzzy partition:

$$\begin{bmatrix} \mu_{ij} \in [0,1] \\ \end{bmatrix}, \ 0 < \sum_{j=1}^{N} \mu_{ij} < N \ , \ \sum_{i=1}^{C} \mu_{ij} = 1$$

➡ The Objective function is

$$J_{P, U, D} = \sum_{i=1}^{C} \sum_{j=1}^{N} \mu_{ij}^{m} d^{2}(x_{j}, P_{i})$$

- OFCM algorithm (Bezdek (Bez81))
 - √ step 1 (Initialization)
 - Fix 2 ≤ C < N, 1 ≤ m < ∞, initialize U(0)
 - √ step 2 (Prototype adaptation)
 - Calculate the C prototypes P_i
 - √ step 3 (Update the C-partition)
 - Update the C-partition matrix **U**(t)
 - √ step 4 (Termination)
 - Repeat steps 2-4 until ΔU<ε

$$P_{i} = \frac{\sum_{j=1}^{N} (\mu_{ij})^{m} x_{j}}{\sum_{j=1}^{N} (\mu_{ij})^{m}}$$

$$\mu_{ij} = \frac{1}{\sum\limits_{k=1}^{C} \left(\frac{d^2(x_j, P_i)}{d^2(x_j, P_k)}\right)^{\frac{1}{m-1}}}$$

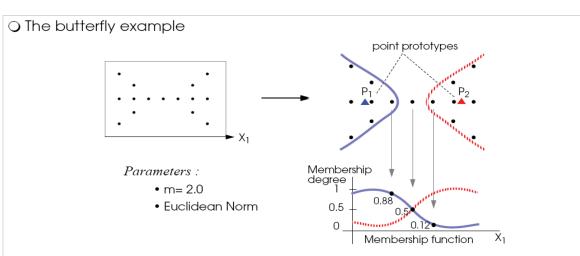
- ➡ transition between full membership and no membership is gradual rather than abrupt.
- $ightharpoonup \mu_{ii}$ represent membership degrees
- **→** soft decisions on class assignments
- Parameters of Fuzzy C-means:
 - **C**: Number of clusters
 - **U(0)**: Initial C-partition
 - \rightarrow $\mathbf{d}^2(x_i, P_i) = (x_i P_i)^T A (x_i P_i)$: "distance measure"
 - If A = Identity matrix then \mathbf{d}^2 is the Euclidean Norm
 - **m** is the weighting exponent called the "fuzzifier"
 - When m→1, Fuzzy C-Means solution become hard.
 - to control the "fuzziness" of the resulting clusters



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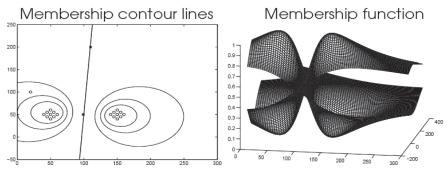
_Chap. 13 | Fuzzy clustering: Fuzzy C-Means



- Discussion
 - → In FCM clustering every point belongs to every cluster to different degrees (<=> constrained fuzzy partition)
 - Minimization of the error propagation during the iterative optimization (<=> soft decision in each iteration)



Example



- O Interpretation
 - Memberships can be interpreted as between class degrees of sharing
 - The centers (prototypes) do not coincide with the true centers of the clusters
 - ➡ Influence of noise points
- Useful for

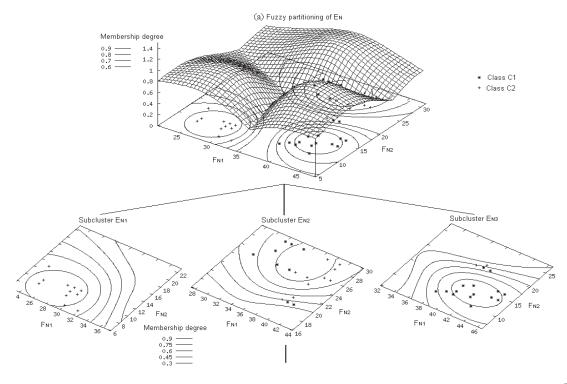
the discrimination of clusters → extraction and modeling of the best boundaries between clusters



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_Chap. 13 | Fuzzy clustering: Fuzzy C-Means / example





 \implies Based on a unconstrained fuzzy partition: $\sum p_{jj}$



➡ The Objective Function is

$$J_{P,\ U,\ X} = \sum_{i=1}^{C} \sum_{j=1}^{N} \mu_{ij}^{\ m} d^{2}(x_{j}, P_{i}) + \sum_{i=1}^{C} \eta_{i} \sum_{j=1}^{N} (1 - \mu_{ij})^{m}$$

- O Algorithm (Krishnapuram&Keller (Kri94a) (Kri93b))
 - √ step 1 (Initialization)
 - Fix 2 ≤ C < N, 1 ≤ m < ∞, initialize U(0)
 - √ step 2 (Prototype adaptation)
 - Calculate the C prototypes P_i
 - √ step 3 (Update the C-partition)
 - Update the C-partition matrix **U**(t)
 - √ step 4 (Termination)
 - Repeat steps 2-4 until $\Delta U < \epsilon$

$$P_{i} = \frac{\sum_{j=1}^{N} (\mu_{ij})^{m} x_{j}}{\sum_{j=1}^{N} (\mu_{ij})^{m}}$$

$$\mu_{ij} = \frac{1}{1 + \left(\frac{d^2(x_j, P_i)}{\eta_i}\right)^{\frac{1}{m-1}}}$$

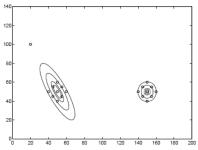
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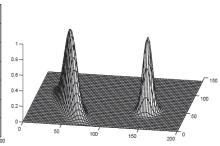
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_Chap. 13 | Fuzzy clustering: Possibilistic Clustering

O Example





Membership contour lines

Membership function

- O Interpretation
 - Memberships can be interpreted as degrees of typicality (absolute numbers)
 - The centers (prototypes) coincide with the "true" centers of the clusters
 - **➡** Low influence of Noise points
- Useful for

the intrinsic characterization of each clusters



"the determination of the optimal number of clusters present in the data is a difficult problem"

- Cluster validity criterion
 - Many different criterions of cluster validity:
 - often based on a measure of compactness and separability of the clusters.
- Different approaches
 - → Iterative clustering:
 - try successively different values of C and evaluate the validity
 - ➡ Progressive clustering:
 - start with one cluster and try progressively to extract a new cluster
 - → Agglomerative clustering:
 - start with many clusters and agglomerate the nearest clusters according to a neightborhood criterion.

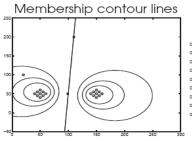


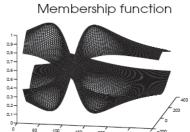
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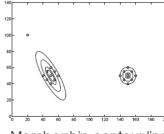
_Chap. 13 | Fuzzy clustering: two different goals

O Fuzzy C-means





Possibilistic clustering



0.2-0.2-0.50 1500 150 200

Membership contour lines

Membership function



"The extraction of shell-like clusters (with no interior points) needs the redesigning of the **distance** measure and/or of the **prototype** of each cluster."

O Example: The fitting of linear structure (e.g. lines)



O Example: The fitting of circular shell

distance:
$$d^2(x_j, c_i) = (\|x_j - c_i\| - r_i)^2$$
 prototype: (c_i, r_i)

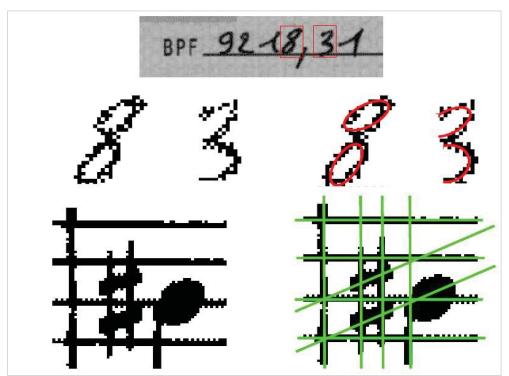
■ Useful for the detection of boundaries and shapes of objects from images



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_Chap. 13 | Fuzzy clustering: Examples





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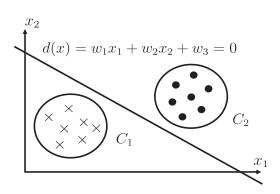
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_Chapitre 15

Classification: Linear Discriminant Functions

_chap. 15 | Classification with Linear Discriminant Functions

- Pattern $x = (x_1, x_2, \dots, x_n) \Longrightarrow n\mathbb{R}^n$ in the n-dimensional vector space
- i.e. nume N:al features
- Assumption: $x_i, 1 \le i \le n$
 - Classes take separable regions which can be separated by linear discriminant functions
 - Parametric models





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chap. 15 | Classification with Linear Discriminant Functions

- How does it work?
 - Labeled training data
 - Calculate discriminant function (e.g., perceptron algorithm)
- Discriminant function

$$d(x) = w_1 x_1 + \dots + w_n x_n + w_{n+1} = w x^t = 0$$

• For an unknown pattern : x

$$x \in \begin{cases} C_1, & \text{if } d(x) > 0\\ C_2, & \text{if } d(x) < 0\\ \text{reject}, & \text{if } d(x) = 0 \end{cases}$$

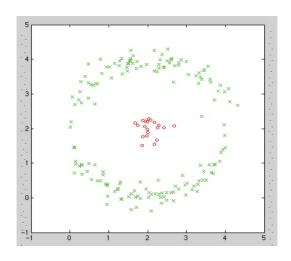


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__Chap. 15 | Linear Discriminant Functions — Generalization

- Linear discriminant functions are not always sufficient
 - i.e. non linear hyperplanes are needed in \mathbb{R}^r





Linear disriminant function

$$d(x) = w_1 x_1 + \dots + w_n x_n + w_{n+1}$$

Generalized discriminant function

$$d(x) = w_1 f_1(x) + \dots + w_m f_m(x) + w_{m+1}$$

= $w(x^*)^t$

With

$$w = (w_1, \dots, w_m, w_{m+1})$$

 $x^* = (f_1(x), \dots, f_m(x), 1); \quad f_1(x), \dots, f_m(x) : \text{functions}$

- Procedure
 - Reduce any arbitrary discriminant function of the above mentioned form to the linear form by transforming the given pattern by application of functions into f(x)
 - \blacksquare In general x^* , i.e. to enable linear separability transform patterns into a space of higher dimension. $m\gg n$



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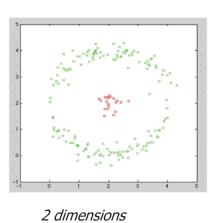
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_Chap. 15 | Linear Discriminant Functions — Generalization

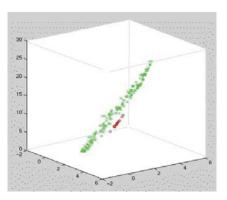
• Example of function

f(x)

[Thierry Artières]



 $(x,y) \rightarrow (x,y,x^2+y^2)$



3 dimensions

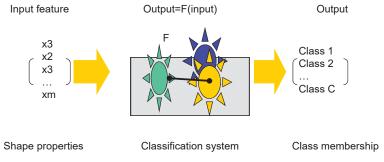


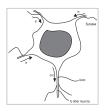
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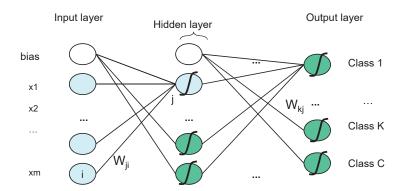
_Chapitre 16 Neural Networks

_Chap. 16 | Neural Networks









Input of a neural j of the layer 0 f: activation function (example sigmoid):

$$a_j = \sum_{i=1}^m w_{ji} x_i + w_{j0}$$



Output of neural j

$$y_j = f(a_j)$$

Input of neural K

$$a_k = \sum_{i=1}^n w_{kj} y_j + w_{k0}$$

Output of neural k

$$z_k = f(a_k)$$

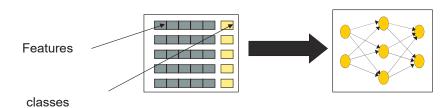
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_chap. 16 | MLP: Learning and generalization

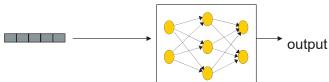
- Learning and generalization capacities
 - Learning
 - consists of presenting an input pattern and modifying the network parameters (weights) to reduce distances between the computed output and the desired output



Input data base

Classifieur

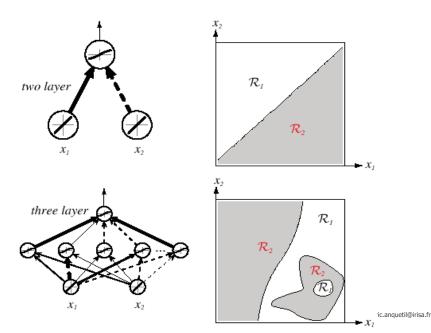
- Generalization / Feedforward
 - consists of presenting a pattern to the input units and passing the signals through the network in order to get outputs units





- MLP: Universal approximator: [A. Kolmogorov]
 - "Any continuous function from input to output can be implemented in a three-layer net, given sufficient number of hidden units, proper nonlinearities, and weights."
 - →Any function from input to output can be implemented as a three-layer neural network

[Duda, PHart, Stork, "Pattern Classification"]





_Chap. 16 | MLP: Learning

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- The aim
 - Construction of a network :
 - to define the nonlinear functions and the weight values
- The Learning process (supervised)
 - Some empirical choices
 - Number of neural and layers
 - Activation functions
 - Principles
 - Present the network a number of inputs and their corresponding outputs
 - See how closely the actual outputs match the desired ones
 - Modify the parameters to better approximate the desired outputs

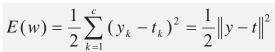


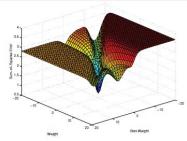
Principle

- The error signal is obtained from the comparison between the target and estimated signal.
- The error signal is propagated layer by layer from the output layer to the input layer to adaptively adjust all weights in the MLP.

Back-propagation (BP) algorithm

- Let t_k be the k-th target (or desired) output and y_k be the k-th computed output with k = 1, ..., c and w represents all the weights of the network
- The training error to minimize:
- Goal:
 We goes through the weight space to find the point corresponding to the minimum of the error
- Method: gradient descent







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_chap. 16 | MLP: Back-propagation (BP) algorithm

The backpropagation learning rule is based on gradient descent

$$\frac{\partial E}{\partial w} = \nabla E[\mathbf{w}] \equiv \left[\frac{\partial E}{\partial w_0}, \frac{\partial E}{\partial w_1}, \dots, \frac{\partial E}{\partial w_p}\right]$$

- Going back from "output" to "input":
 - 1 Calculate the derivatives of the error with respect to weights
 - 2 Using these derivatives for adjust the weights

$$\mathbf{w}^{(\tau+1)} \leftarrow \mathbf{w}^{(\tau)} - \eta \nabla E[\mathbf{w}^{(\tau)}]$$

$$\Delta w = -\eta \, \frac{\partial E}{\partial w}$$

where $\boldsymbol{\eta}$ is the learning rate which indicates the relative size of the change in weights



_Chap. 16 | MLP: Back-propagation (BP) algorithm

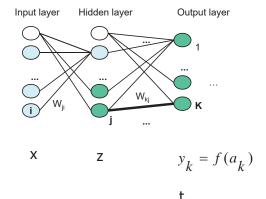
 Sensitivity deduce from the gradient descent hidden-to-output (j → k) weights

$$\frac{\partial E}{\partial w_{kj}} = \frac{\partial E}{\partial y_k} \frac{\partial y_k}{\partial e_k} \frac{\partial e_k}{\partial w_{kj}} = \delta_k z_j \text{ (because } e_k = w_{kj} z_j, \text{ partial input of } a_k)$$

$$\delta_k = \frac{\partial E}{\partial y_k} \frac{\partial y_k}{\partial e_k} = (y_k - t_k) f'(a_k)$$

$$\Delta w_{kj} = -\eta \delta_k z_j$$

$$e_k = \mathbf{w}_{kj} \mathbf{z}_j$$
: partial input of \mathbf{k} $(\mathbf{j} \to \mathbf{k})$
 y_k output of \mathbf{k}
 z_j output of \mathbf{j}





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_Chap. 16 | MLP: Back-propagation (BP) algorithm

- Sensitivity deduce from the gradient descent at a hidden unit (i→j):
 - the sum of the individual sensitivities at the output units weighted by the hidden-to-output weights w_{ki}; all multipled by f'(a)

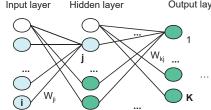
$$\delta_{j} \equiv f'(a_{j}) \sum_{k=1}^{c} w_{kj} \delta_{k} \qquad \Delta w_{ji} = -\eta \delta_{j} x_{i}$$

Backpropagation algorithm

The weights are initialized with pseudo-random values and are changed in a direction that will reduce the error:

| Input layer | Hidden layer | Output laye

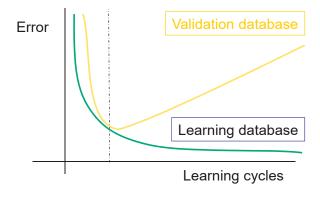
$$\label{eq:begin_def} \begin{array}{ll} \underline{\text{Begin}} & \underline{\text{initialize}} & n_{_{\! H}}; \text{ w, } \eta, \text{ m=0} \\ \underline{\text{do}} & \text{m} = \text{m} + 1 \\ & x^{\text{m}} \leftarrow \text{randomly chosen pattern} \\ & w_{_{ji}} = w_{_{ji}} - \eta \delta_{_{j}} x_{_{i}}; \text{ } w_{_{kj}} = w_{_{kj}} - \eta \delta_{_{k}} z_{_{j}} \\ \underline{\text{until}} & \text{Stopping criterion} \\ \underline{\text{return}} & \text{w} \\ \underline{\text{End}} \end{array}$$





__Chap. 16 | MLP: Learning with validation

- Learning with validation (to avoid overfitting)
 - Two Learning Databases:
 - One for the learning phase
 - One for the validation of the learning
 - Test Database
 - Generalization evaluation



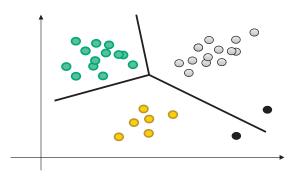


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_Chap. 16 | MLP: knowledge modeling

- knowledge modeling
 - Easy/Powerful learning
 - Knowledge are distributed il all the weight of network
 - Black-box system
 - Discriminative learning: with Hyper planes



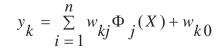


Input layer 1 hidden layer Output layer

bias X^1 X^2 $X = X^2$ $X = X^$

 Φ: radial activation function distance measure to the prototype (linear combination)





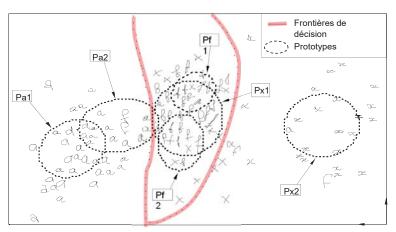


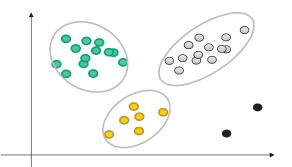
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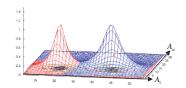
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_Chap. 16 | RBFNN : Learning

- Two approaches for the learning phase:
 - 1/ Globally by backpropagation
 - 2/ In two phases
 - a/ clustering to initialize the centers of the Radial Basis Function (RBF)
 - b/ Output Weights
 - learning by Least Mean Square (LMS)







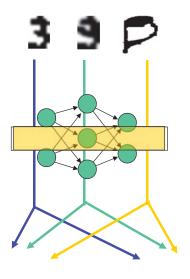


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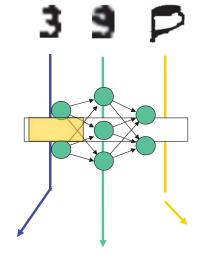
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_Chapitre 17 **Reject Option**

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Good recognition Confusion



Good recognition Confusion

Reject

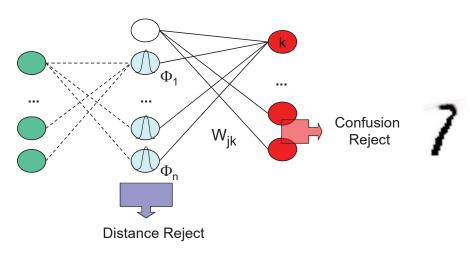
Distance Reject

Unknown input



_chap. 17 | Reject option with thresholds

- With MLP : only confusion reject
- With RBFNN: both confusion and distance reject



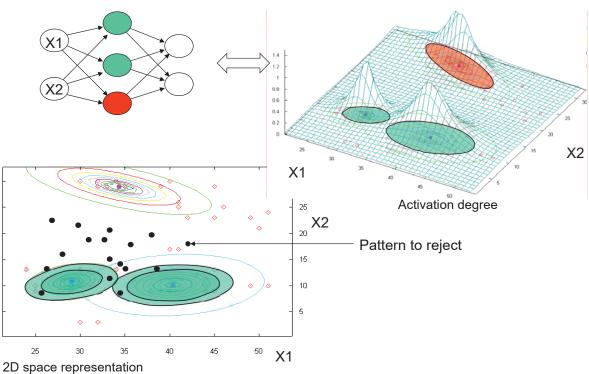




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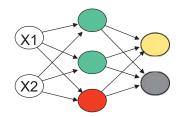
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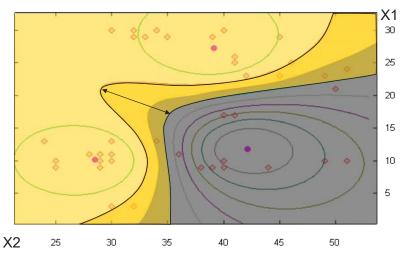
_Chap. 17 | Distance reject / with thresholds





_chap. 17 | Confusion reject / with thresholds



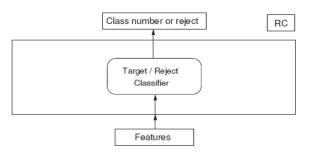




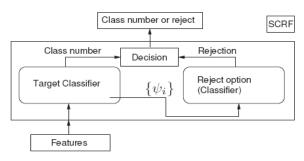
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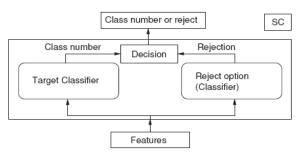
_Chap. 17 | Reject option: Main approaches (distance reject)



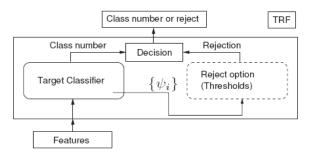
(a) a Reject Class in the target classifier



(c) a Specialized Classifier on the Reliability Functions $\{\psi_i\}$



(b) a Specialized Classifier on the feature space



(d) Thresholds on the Reliability Functions $\{\psi_i\}$ [Mouchère07]



__Chap. 17 | Evaluation of Recognition Systems

Evaluation measure

re		Desired Positive		Desired Negative	
Test Outcome	Positive N _E	True Positive	N_E^A	False Positive	N_R^A
	Negative N _R	False negative	N_E^R	True Negative	N_R^R

- Recognition/Error Rates
 - TAR: True Acceptance Rate
 - FAR: False Acceptance Rate

$$TAR = \frac{N_E^A}{N_E}$$

$$FAR = \frac{N_R^A}{N_R} \bigg| \bigg|$$

- Accuracy Rates ("fiabilité")
 - Global performance point of view

- $Accuracy = \frac{N_E^A + N_R^A}{N_E + N_R}$
- Recall = TAR

- recall ("rappel")
 - information retrieval → the number of relevant documents retrieved by a search / the total number of existing relevant documents
 - Precision = $\frac{N_E^A}{N_E^A + N_R^A}$

- Precision ("précision")
 - the number of items correctly labeled ∈the positive class / the total number of elements labeled ∈ the positive class
 - information retrieval → number of relevant documents retrieved by a search divided by the total number of documents retrieved by that search



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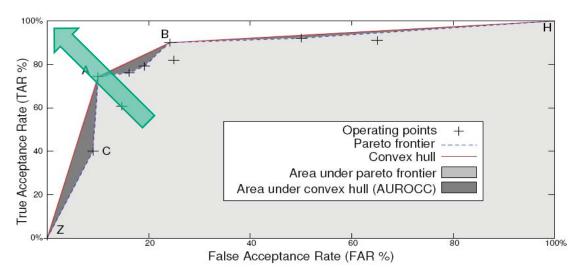
182

_chap. 17 | Evaluation: distance reject / evaluation

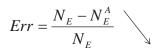
- Evaluation of outlier(distance) rejection
 - ROC curves (Receiver Operating Characteristics)
 - The optimum operating point is the top left point

$$TAR = \frac{N_E^A}{N_E}$$

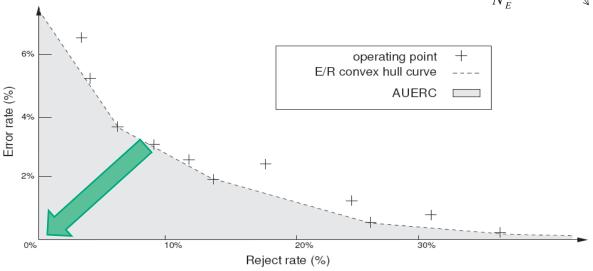
$$FAR = \frac{N_R^A}{N_R}$$



- Evaluation of confusion rejection
 - error/reject curve (E/R curve)
 - The optimum operating point is the bottom left point



$$Rej = \frac{N_E^R}{N_E}$$





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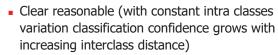
Version 1.0

_Chapitre 18
Support Vector Machines

Volker Märgner Haikal El Abed

- Origin in statistic learning theory; class of optimal classifiers
 - Main problem of the statistic learning theory: Generalization ability
 - When does a low training error cause a low real error?
- Large/Max-Margin classifier / Linear Separable Classes

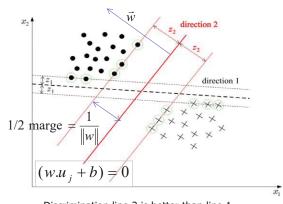
• With SVM a discriminating hyperplane with maximal border is searched. Optimal: that with the largest of all possible discrimination planes



 Theoretically SVM are justified by statistic learning theory

$$X = \{u_j, c_j\}_j \text{ where } c_j = \begin{cases} +1 & \text{if } u_j \in C_1 \\ -1 & \text{if } u_j \in C_2 \end{cases}$$
find **w** and *b* such that
$$\mathbf{w} u_j + b \ge +1 \text{ for } c_j = +1$$

$$\mathbf{w} u_j + b \le -1 \text{ for } c_j = -1$$
which can be rewritten as
$$c_j (\mathbf{w} u_j + b) \ge +1$$



Discrimination line 2 is better than line 1



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_Chap. 18 | Basic notion of Support-Vector-Machines (SVM)

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Volker Märgner

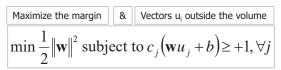
Haikal El Abed

- Training max-Margin classifier
 - Constraint optimization (two classes C₁ et C₂ (+1,-1))
 - To find support vector /hyperplan parameters
 - Margin to closest +1 (u₁) and -1 (u₂) points to be 1 $-1(w.u_2 + b) = 1$

$$+1(w u + h) = 1$$

$$+1(w.u_1 + b) = 1$$

- Maximize
- Minimize



direction 1 1/2 marge Discrimination line 2 is better than line 1

Unconstrained problem using Lagrange multipliers



- Classification
 - Given unknown vector u, predict class (-1 or 1) as follows:

$$h(u) = sign\left(\sum_{i=1}^{k} \alpha_i y^i x^i \cdot u + b\right) = sign\left(w.u + b\right)$$

- The sum is over k support vectors (xi,yi)
- If Not linearly separable (Soft Margin)
 - Vectors u_i outside the volume, which are correctly classified (c_i) i.e.

$$c_j(w.u_j + b) \ge 1$$

$$\longrightarrow \xi_i = 0$$

 Vectors inside the volume, which are correctly classified, i.e.

$$0 \le c_i(w.u_i + b) < 1$$

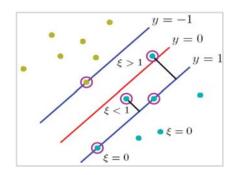
$$\longrightarrow 0 < \xi_i \le 1$$

Vector, which are wrongly classified

$$c_i(w.u_i + b) < 0$$

$$\longrightarrow \xi_j > 1$$

 Parameter C can be viewed as a way to control overfitting: it "trades off" the relative importance of maximizing the margin and fitting the training data.



If no discrimination line exists (slack variables)

$$c_j(w.u_j + b) \ge 1 - \xi_j$$

minimi

$$\frac{1}{2} \|w\|^2 + C \sum_{j=1}^m \xi_j$$

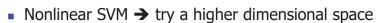
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 $(x,y) \rightarrow (x,y,x^2+y^2)$



__Chap. 18 | Basic notion of Support-Vector-Machines (SVM)



Problem: Very high dimension of the feature space

$$\mathbb{R}^n \Rightarrow \mathbb{R}^m, m = O(n^p)$$

Advantage with SVM

Recognition depends only on dot product of unknown with sample

Trick with kernel functions:

Originally in

only \mathbb{R}^n r products

 $neces x_i x_j$

New in

only \mathbb{R}^m :r product

 $\Psi(x_i)\Psi(x_i)$ y



• $\Psi(x_i)\Psi(x_j)$ be calculated explicitly, but can be expressed with reduced complexity with kernel functions $K(x_i,x_j)=\Psi(x_i)\Psi(x_j)$



$$\Psi \cdot \mathbb{R}^2 \Rightarrow \mathbb{R}^6$$

$$\Psi((y_1, y_2)) = (y_1^2, y_2^2, \sqrt{2}y_1, \sqrt{2}y_2, \sqrt{2}y_1y_2, 1)$$

$$K(x_i, x_j) = (x_i x_j + 1)^2 = \Psi(x_i)\Psi(x_j)$$

$$\mathbb{R}^6$$



- Strengthens of SVM
 - SVM supplies very good classification results according to present expertise; for a set of tasks it is considered as the "Top Performer"
 - Sparse-representation of the solution by support vectors
 - **Easily applicable**: small parameter set, no a-priory-knowledge necessary
 - Theoretical statements about results: global optimum, generalization ability
- Weaknesses of SVM
 - Multi-class approach still subject of research (extension to more classes e.g. with a hierarchical procedure, where one certain class and the remainder are regarded as two classes)
 - Slow and memory-intensive learning
 - Tuning of SVMs is still a "black art": Selection of a specific kernel and suitable parameters is made by tests



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